

raymond

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1 examples/Balls.frag

```

#version 330 compatibility

/*
Raymond - a physics-inspired ray tracer for Fragmentarium
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   License GPL3+ <http://www.gnu.org/licenses/>
   */

#include "Raymond-sRGB.frag"
10 #include "Raymond.frag"

uint hash(uint a)
{
    return hash_burtle_9(a);
15 }

Ray camera(Random PRNG, Camera C, vec2 coord, out float intensity)
{
    return pinhole(PRNG, C, -coord, pinhole_uniforms(), intensity);
20 }

float raytrace(Random PRNG, Ray V, out Hit h)
{
    return raytrace_de(PRNG, V, raytrace_de_uniforms(), h);
25 }

vec3 film(Random PRNG, float wavelength, float intensity)
{
    return xyz2rgb(observer(wavelength) * intensity);
30 }

float screen(vec4 tex, float wavelength)
{
    return 0.0;
35 }

vec4 light(Random PRNG, vec3 from, vec3 dir)
{
    return vec4(0.0);
40 }

#define SCENE(hit,surface,scene_tag) \
hit scene(scene_tag tag, Random PRNG, Ray V) \
45 { \
    surface G = Plane(tag, Identity(), V, Z, 0.0); \
    return Union6 \
        ( Light(Invert(Sphere(tag, Scale(50.0), V)), V, \
          D65(V.wavelength) * 5.0 * pow(V.origin.z / 50.0, 8.0)) \
50      , Glass (srand(PRNG, 1), Sphere(tag, Translate(vec3(0.0,-4.5,1.0))), V), V) ↵ \
        , Quartz (srand(PRNG, 2), Sphere(tag, Translate(vec3(0.0,-1.5,1.0))), V), V) ↵ \
        , Water (srand(PRNG, 3), Sphere(tag, Translate(vec3(0.0, 1.5,1.0))), V), V) ↵ \
        ↵ \

```

```

        , Diffuse(srand(PRNG, 4), Sphere(tag, Translate(vec3(0.0, 4.5,1.0)), V), V, ↗
        ↘ 0.5) \
    , Checkerboard \
55    ( V.origin \
        , Diffuse(srand(PRNG, 5), G, V, 0.3) \
        , Diffuse(srand(PRNG, 6), G, V, 0.7) \
        ) \
    ); \
60 }

SCENE(Hit, Surface, Scene_HIT)
#if 1
// fast
65 SCENE(float, float, Scene_DE)
#else
// slow
float scene(Scene_DE tag, Random PRNG, Ray V)
{
70     Scene_HIT HIT;
    return scene(HIT, PRNG, V).surface.de;
}
#endif

75 #preset Default
FOV = 0.575
Eye = 8.703398,3.894242,3.333333
Target = 1.140564,0.6462541,0.3816794
Up = -0.3986355,-0.3137904,0.7589191
80 Steps = 100
Depth = 25
Acne = -16.51064
Aperture = 0.0299999
Size = 35
85 Wavelengths = 300,780
Exposure = 2
#endpreset

```

2 examples/Bubbles.frag

```

#version 330 compatibility

/*
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*/

#include "Raymond-sRGB.frag"
10 #include "Raymond.frag"

#group Bubble
uniform float Thickness; slider[100.0,1000.0,10000.0]

15 // render as lights instead of bubbles
const bool DEBUG = false;

uint hash(uint a)

```

```

{
20   return hash_burtle_9(a);
}

Ray camera(Random PRNG, Camera C, vec2 coord, out float intensity)
{
25   return pinhole(PRNG, C, -coord, pinhole_uniforms(), intensity);
}

float raytrace(Random PRNG, Ray V, out Hit h)
{
30   return raytrace_de(PRNG, V, raytrace_de_uniforms(), h);
}

vec3 film(Random PRNG, float wavelength, float intensity)
{
35   return xyz2rgb(observer(wavelength) * intensity);
}

float screen(vec4 tex, float wavelength)
{
40   return CRT(sRGB2linear(tex.rgb), wavelength);
}

vec4 light(Random PRNG, vec3 from, vec3 dir)
{
45   return vec4(0.0);
}

vec4 bubble(vec3 origin, int n)
50 {
    vec3 lo = floor(origin);
    vec3 md = vec3(lo) + vec3((ivec3(n) & ivec3(1, 2, 4)) >> ivec3(0, 1, 2));
    // pseudo-random hash of integer grid coordinates
    Random PRNG2;
55   PRNG2.seed = hash(md);
    PRNG2.index = 0u;
    Random PRNG3;
    PRNG3.seed = hash(md.xy);
    PRNG3.index = 0u;
60   vec4 posr;
    posr.xyz = uniform3(PRNG2) - vec3(0.5) + md;
    posr.w = uniform1(PRNG3) * 0.125 * (0.9 - smoothstep(4.0, 6.0, length(posr.xyz ↵
        ↵ )))
    return posr;
}
65

// https://en.wikipedia.org/wiki/Cubic_Hermite_spline#↵
    ↵ Interpolation_on_the_unit_interval_with_matched_derivatives_at_endpoints
vec4 bubble4(vec3 origin, int n, float t)
{
    const mat4 M = mat4
70   ( 0.0, 2.0, 0.0, 0.0
      , -1.0, 0.0, 1.0, 0.0
      , 2.0, -5.0, 4.0, -1.0
      , -1.0, 3.0, -3.0, 1.0

```

```

    ) / 2.0;
75   vec4 u = vec4(1.0, t, t * t, t * t * t);
    mat4 p = mat4
        ( bubble(origin - Z, n)
          , bubble(origin, n)
          , bubble(origin + Z, n)
80      , bubble(origin + Z * 2.0, n)
        );
    return u * transpose(M) * transpose(p);
}

85  #define SCENE(hit,surface,scene_tag) \
    hit scene(scene_tag tag, Random PRNG, Ray V) \
    { \
        float t = time / 5.0; \
        float FPS = 25.0; \
90     float shutter = 0.25 / FPS; \
        t += shutter * halton1(srand(PRNG, 5)); \
        t -= floor(t); \
        hit h = SkyBox(tag, Identity(), V); \
        for (int n = 0; n < 8; ++n) \
95     { \
            for (int m = -1; m < 2; ++m) \
            { \
                vec4 posr = bubble4(V.origin - float(m) * Z, n, t); \
                if (posr.w > 0.0) \
100            { \
                    float thick = Thickness * clamp(1.0 - (V.origin.z - posr.z) / posr.w, ↵
                        ↵ 0.01, 1.99); \
                    vec2 nk = Water_nk(V.wavelength); \
                    surface ball = Sphere(tag, compose(Scale(posr.w), Translate(posr.xyz)), ↵
                        ↵ V); \
                    h = Union(h, DEBUG ? Light(ball, V, D65(V.wavelength)) : SoapBubble \
105                ( srand(PRNG, 4 + n * 3 + m + 1) \
                    , ball \
                    , V \
                    , thick \
                    , nk \
110                )); \
            } \
        } \
    } \
    return h; \
115 }

SCENE(Hit, Surface, Scene_HIT)
#if 1
// 16fps / 3.8fps / 1.9fps
120 // fast
SCENE(float, float, Scene_DE)
#else
// 15fps / 3.8fps / 1.9fps
// slow
125 float scene(Scene_DE tag, Random PRNG, Ray V)
{
    Scene_HIT HIT;
    return scene(HIT, PRNG, V).surface.de;
}

```

```

    }
130 #endif

    #preset Default
    Exposure = 100
    Steps = 100
135 FOV = 1
    Eye = 0,0,0
    Target = 0,1,1
    Up = 0,0,1
    Background = ../images/Berlin.equi.jpg
140 Distance = 100
    Depth = 10
    Acne = -16
    Aperture = 0.035,0.02
    Size = 35
145 Wavelengths = 300,780
    Thickness = 1000
    #endpreset

```

3 examples/Cubism.frag

```

#version 330 compatibility

/*
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*/

#include "Raymond-sRGB.frag"
10 #include "Raymond.frag"

// animation parameters
const float bpm = 130.0;
const float beats = 512.0;
15 const float seconds = beats / bpm * 60.0;
const float fps = 25.0;
const float shutter = 0.5;

struct Animation
20 {
    Transform A, B, C, D;
    float t1, t2;
};

25 Animation animation(Random PRNG)
{
    float t = (time + shutter / fps * uniform1(PRNG)) / seconds;
    t -= floor(t);
    t *= 2.0;
30 // generate quantized noise
    Random r1, r2, r3, r4;
    r1.seed = hash(vec2(mod(floor(t + 0.0), 2.0), 1.0)); r1.index = 0u;
    r2.seed = hash(vec2(mod(floor(t + 1.0), 2.0), 1.0)); r2.index = 0u;
    r3.seed = hash(vec2(mod(floor(t + 0.5), 2.0), 2.0)); r3.index = 0u;
35 r4.seed = hash(vec2(mod(floor(t + 1.5), 2.0), 2.0)); r4.index = 0u;

```

```

// random unit quaternions (orientations)
vec4 q1, q2, q3, q4;
q1 = normalize(gaussian4(r1));
q2 = normalize(gaussian4(r2));
40 q3 = normalize(gaussian4(r3));
q4 = normalize(gaussian4(r4));
// interpolate
vec4 p1 = slerp(q1, q2, t - floor(t));
vec4 p2 = slerp(q3, q4, t + 0.5 - floor(t + 0.5));
45 // faster layer on top
t *= 4.0;
// generate quantized noise
r1.seed = hash(vec2(mod(floor(t + 0.0), 8.0), 3.0)); r1.index = 0u;
r2.seed = hash(vec2(mod(floor(t + 1.0), 8.0), 3.0)); r2.index = 0u;
50 r3.seed = hash(vec2(mod(floor(t + 0.5), 8.0), 4.0)); r3.index = 0u;
r4.seed = hash(vec2(mod(floor(t + 1.5), 8.0), 4.0)); r4.index = 0u;
// random film thicknesses
float t1 = mix(100.0, 1000.0, uniform1(r1));
float t2 = mix(100.0, 1000.0, uniform1(r2));
55 float t3 = mix(100.0, 1000.0, uniform1(r3));
float t4 = mix(100.0, 1000.0, uniform1(r4));
float a1 = mix(t1, t2, t - floor(t));
float a2 = mix(t3, t4, t + 0.5 - floor(t + 0.5));
// return
60 Animation a;
a.A = Rotate(p1);
a.B = Rotate(p2);
a.C = Rotate(-p1);
a.D = Rotate(-p2);
65 a.t1 = a1;
a.t2 = a2;
return a;
}

70 Animation Anim;

uint hash(uint a)
{
    return hash_burtle_9(a);
75 }

Ray camera(Random PRNG, Camera C, vec2 coord, out float intensity)
{
    // initialize animation once
80 Anim = animation(srand(PRNG, 1));
    return pinhole(srand(PRNG, 2), C, -coord, pinhole_uniforms(), intensity);
}

float raytrace(Random PRNG, Ray V, out Hit h)
85 {
    return raytrace_de(PRNG, V, raytrace_de_uniforms(), h);
}

vec3 film(Random PRNG, float wavelength, float intensity)
90 {
    return xyz2rgb(observer(wavelength) * intensity);
}

```



```

float screen(vec4 tex, float wavelength)
95 {
    return CRT(sRGB2linear(tex.rgb), wavelength);
}

vec4 light(Random PRNG, vec3 from, vec3 dir)
100 {
    return vec4(0.0);
}

Hit scene(Scene_HIT tag, Random PRNG, Ray V)
105 {
    // glitch the ray tracing
    Ray U;
    U = V;
110    U.origin = forwardP(Anim.D, U.origin);
    U.direction = forwardN(Anim.D, U.direction);
    Hit h1 = ThinFilm(MengerSponge(tag, Anim.A, U, 3), V, Anim.t1, 1.0);
    U = V;
    U.origin = forwardP(Anim.C, U.origin);
115    U.direction = forwardN(Anim.C, U.direction);
    Hit h2 = ThinFilm(MengerSponge(tag, Anim.B, U, 3), V, Anim.t2, 1.0);
    return Union3
        ( Light(Invert(Sphere(tag, Scale(100.0), V)), V, D65(V.wavelength))
          , h1
120          , h2
        );
}

float scene(Scene_DE tag, Random PRNG, Ray V)
125 {
    Scene_HIT HIT;
    return scene(HIT, PRNG, V).surface.de;
}

130 #preset Default
    FOV = 0.4
    Eye = 0,0,0
    Target = 1,0,0
    Up = 0,0,1
135    Exposure = 2
    Steps = 3
    Depth = 15
    Acne = 0
    Aperture = 0.1,0.1
140    Size = 35
    Wavelengths = 300,780
#endpreset

```

4 examples/Lettuce.frag

```
#version 330 compatibility
```

```

/*
Raymond - a physics-inspired ray tracer for Fragmentarium

```

```

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   */

#include "Raymond-sRGB.frag"
10  #include "Raymond.frag"

#include "Raymond-Lettuce.frag"

uniform bool Colour; checkbox[true]

15  // pseudo-random hash
   uint hash(uint a)
   {
       return hash_burtle_9(a);
20  }

// pinhole camera
Ray camera(Random PRNG, Camera C, vec2 coord, out float intensity)
{
25  return pinhole(PRNG, C, -coord, pinhole_uniforms(), intensity);
}

// distance estimator raytracer
float raytrace(Random PRNG, Ray V, out Hit h)
30  {
    return raytrace_de(PRNG, V, raytrace_de_uniforms(), h);
}

// CIE observer
35  vec3 film(Random PRNG, float wavelength, float intensity)
{
    if (Colour)
        return xyz2rgb(observer(wavelength) * intensity);
    else
40  return xyz2rgb(vec3(fp4plus(wavelength) * intensity));
}

// sRGB texture using CRT model
float screen(vec4 tex, float wavelength)
45  {
    return CRT(sRGB2linear(tex.rgb), wavelength);
}

// scene definition
50  #define SCENE(hit,surface,scene_tag) \
hit scene(scene_tag tag, Random PRNG, Ray V) \
{ \
    return Union4 \
        ( Mirror(Invert(Sphere(tag, Scale(8.0), V)), V, Screen_hump(vec3(400.0, 4
          ↳ 300.0, 1.0), V.wavelength)) \
55  , Light(Sphere(tag, Translate(vec3(2.0, 5.5, 5.0)), V), V, 500.0 * D65(V.4
          ↳ wavelength)) \
        , Diffuse(srand(PRNG, 2), Plane(tag, Identity(), V, Z, 0.0), V, Screen_hump(4
          ↳ vec3(700.0, 100.0, 1.0), V.wavelength)) \
        , Diffuse(srand(PRNG, 3), Lettuce(tag, Translate(vec3(0.0, 0.0, 2.0)), V, 4
          ↳ 16), V, Screen_hump(vec3(580.0, 200.0, 1.0), V.wavelength)) \

```

```

    ); \
}
60 //      , Light(Plane(tag, Identity(), V, -Z, -6.0), V, 1.0 * D65(V.wavelength)) \

vec4 light(Random PRNG, vec3 from, vec3 dir)
{
    vec3 lpos = vec3(2.0, 5.5, 5.0);
65    vec3 ldir = lpos - from;
    float t = cos(asin(1.0 / length(ldir)));
    float s = dot(normalize(ldir), normalize(dir));
    if (length(from) >= 7.999)
    {
70    if (s > t) return vec4(normalize(dir), 1.0); else return vec4(0.0);
    }
    vec3 to = normalize(gaussian3(srand(PRNG, 5))) + lpos;
    return vec4(normalize(to - from), (1.0 - t) / 2.0);
}

75 // scene for DE with lighting
SCENE(Hit, Surface, Scene_HIT)

#ifdef DEBUG
80 // scene for DE only (fast)
SCENE(float, float, Scene_DE)

#else
85 // reuse DE with lighting (slow)
float scene(Scene_DE tag, Random PRNG, Ray V)
{
    Scene_HIT HIT;
90    return scene(HIT, PRNG, V).surface.de;
}

#endif

95 #preset Default
    Exposure = 1
    FOV = 1
    Eye = 4,2,4
100    Target = 0.5,0,2
    Up = 0,0,1
    Background =
    Distance = 100
    Steps = 100
105    Depth = 10
    MinDist = -16
    Acne = -12
    Aperture = 0.0,0.0
    Size = 1000
110    Wavelengths = 300,780
    Colour = true
#endpreset

```

5 examples/Mandelbrot.frag

```

#version 330 compatibility

/*
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*/

#include "Raymond-sRGB.frag"
10  #include "Raymond.frag"

#group Mandelbrot
// maximum period for atoms and domains
uniform int Period; slider[1,1,128]
15  // minimum size of atoms and domains
uniform float MinSize; slider[-24,-10,1];
// maximum iteration count for exterior
uniform int Iterations; slider[1,1,1000];
// thickness of exterior fringe
20  uniform float Thickness; slider[-24,-10,1];

// standard preamble

uint hash(uint a)
25  {
    return hash_burtle_9(a);
}

Ray camera(Random PRNG, Camera C, vec2 coord, out float intensity)
30  {
    return pinhole(PRNG, C, -coord, pinhole_uniforms(), intensity);
}

float raytrace(Random PRNG, Ray V, out Hit h)
35  {
    return raytrace_de(PRNG, V, raytrace_de_uniforms(), h);
}

vec3 film(Random PRNG, float wavelength, float intensity) {
40  return xyz2rgb(observer(wavelength) * intensity);
}

float screen(vec4 tex, float wavelength)
{
45  return CRT(sRGB2linear(tex.rgb), wavelength);
}

vec4 light(Random PRNG, vec3 from, vec3 dir)
{
50  return vec4(0.0);
}

// Mandelbrot numerics

55  // https://mathr.co.uk/blog/2018-11-17-newtons-method-for-periodic-points.html

```

```

vec2 Mandelbrot_nucleus(vec2 c0, int period)
{
    vec2 c = c0;
    for (int j = 0; j < 16; ++j)
60     {
        vec4 G = cConst(1.0);
        vec4 z = cConst(0.0);
        c0 = c;
        for (int l = 1; l <= period; ++l)
65         {
            z = cSqr(z) + cVar(c);
            if (l < period && period % l == 0)
                G = cMul(z, G);
        }
70     G = cDiv(z, G);
        c = c0 - cDiv(G.xy, G.zw);
        if (! (c != c0)) break;
    }
    return c;
75 }

// https://mathr.co.uk/blog/2016-12-24_deriving_the_size_estimate.html
vec2 Mandelbrot_size(vec2 c, int period)
{
80     vec2 l = vec2(1.0, 0.0);
    vec2 b = vec2(1.0, 0.0);
    vec2 z = vec2(0.0, 0.0);
    for (int i = 1; i < period; ++i)
    {
85         z = cSqr(z) + c;
        l = 2.0 * cMul(z, l);
        b = b + cDiv(vec2(1.0, 0.0), l);
    }
    return cDiv(vec2(1.0, 0.0), cMul(b, cSqr(l)));
90 }

// https://mathr.co.uk/blog/2013-04-01↵
//   ↵ _interior_coordinates_in_the_mandelbrot_set.html
// https://mathr.co.uk/blog/2015-01-26_newtons_method_for_misiurewicz_points.↵
//   ↵ html
vec4 Mandelbrot_attractor(vec2 c, vec2 z_initial, int period)
95 {
    vec4 z = cVar(z_initial);
    vec2 dz = vec2(0.0);
    for (int j = 0; j < 16; ++j)
    {
100         vec4 z0 = z;
        vec4 G = cConst(1.0);
        for (int l = 1; l <= period; ++l)
        {
            z = cSqr(z) + cConst(c);
105             if (l < period && period % l == 0)
                G = cMul(z - z0, G);
        }
        dz = z.zw;
        G = cDiv(z - z0, G);
110         z = cVar(z0.xy - cDiv(G.xy, G.zw));
    }
}

```

```

        if (! (z != z0)) break;
    }
    return vec4(z.xy, dz);
}
115 // trace ray from a nucleus, more stable than trying to do it one jump
vec4 Mandelbrot_attractor_ray(vec2 nucleus, vec2 target, int period)
{
    const int steps = 16;
120    vec4 P = vec4(0.0);
    for (int ray = 1; ray <= steps; ++ray)
    {
        float t = float(ray) / float(steps);
        P = Mandelbrot_attractor(mix(nucleus, target, t), P.xy, period);
125    }
    return P;
}

// https://mathr.co.uk/blog/2013-12-10-atom-domain-size-estimation.html
130 float Mandelbrot_domain_size(vec2 c, int p)
{
    vec4 z = cVar(c);
    float abszq = length(z.xy);
    for (int q = 2; q <= p; ++q) {
135        z = cSqr(z) + cVar(c);
        float abszp = length(z.xy);
        if (abszp < abszq && q < p) {
            abszq = abszp;
        }
140    }
    return abszq / length(z.zw);
}

// main DE function
145 vec3 Mandelbrot(vec3 object, float bg)
{
    // FIXME should be able to take uniforms as arguments
    int maxPeriod = Period;
150    float minSize = pow(2.0, MinSize);
    int maxIters = Iterations;
    float thickness = pow(2.0, Thickness);
    // no transformations supported
    vec2 c = object.xy;
155    vec2 z = vec2(0.0, 0.0);
    // derivative for exterior distance
    vec2 dc = vec2(0.0, 0.0);
    // minimums for atom domains
    vec2 mz = vec2(0.0, 0.0);
160    float mr2 = 1.0 / 0.0;
    // calculate 3x (DE,material,bubblethicknessfactor) for CSG operations
    vec3 back = vec3(bg, 0.0, 0.0);
    if (bg < 0.0)
        return back;
165    vec3 far = vec3(1.0/0.0, 1.0, 0.0);
    vec3 de_nucleus = far;
    vec3 de_domain = far;

```

```

    vec3 de_exterior = far;
    int escaped = 0;
170   int period = 1;
    for (; period <= maxPeriod; ++period)
    {
        dc = 2.0 * cMul(z, dc) + vec2(1.0, 0.0);
        z = cSqr(z) + c;
175   float r2 = dot(z, z);
        if (r2 < 1.5 * mr2)
        {
            vec2 nucleus = Mandelbrot_nucleus(c, period);
            if (period > 1)
180         {
                vec2 atom = cDiv(z, mz);
                float S = Mandelbrot_domain_size(nucleus, period);
                if (S > minSize)
                {
185                 // make a DE-traceable shell out of two surfaces inside each other
                    float a = length(vec3(atom, object.z / S));
                    vec3 d1 = vec3((a - 1.01) * S, 3.0, clamp(object.z / S + 1.0, 0.01, ↵
                        ↵ 1.99));
                    vec3 d2 = vec3(-(a - 0.99) * S, 4.0, 0.0);
                    float d = max(d1.x, d2.x);
190                 if (d < de_domain.x) de_domain = d1.x > d2.x ? d1 : d2;
                }
            }
            if (true)
            {
195                 vec2 atom = Mandelbrot_attractor_ray(nucleus, c, period).zw;
                    float S = 0.5 * length(Mandelbrot_size(nucleus, period));
                    if (S > minSize)
                    {
                        float d = (length(vec3(atom, object.z / S)) - 1.0) * S;
200                     if (d < de_nucleus.x) de_nucleus = vec3(d, 2.0, 0.0);
                    }
                }
            if (r2 < mr2)
            {
205                 mz = z;
                    mr2 = r2;
                }
            if (de_nucleus.x < 0.0)
            {
210                 escaped = -1;
                    break;
                }
        }
        if (r2 > 65536.0)
215     {
            escaped = 1;
            break;
        }
    }
220   if (escaped == 0)
    {
        for (; period <= maxIters; ++period)
        {

```

```

    dc = 2.0 * cMul(z, dc) + vec2(1.0, 0.0);
225    z = cSqr(z) + c;
    float r2 = dot(z, z);
    if (r2 > 65536.0)
    {
230        escaped = 1;
        break;
    }
}
if (escaped == 1)
235 {
    float d = length(z) * log(length(z)) / length(dc);
    d = length(vec2(d, object.z)) - thickness;
    if (d < de_exterior.x) de_exterior = vec3(d, 1.0, 0.0);
}
240 // disjoint union(b, a - b) = union(b, intersection(a, invert(b)))
// this hopefully fixes unsightly issues at atom/domain intersections
if (isnan(de_exterior.x)) de_exterior = back;
if (isnan(de_nucleus.x)) de_nucleus = back;
if (isnan(de_domain.x)) de_domain = back;
245 vec3 solid = de_exterior.x < de_nucleus.x ? de_exterior : de_nucleus;
vec3 bubble = -solid.x > de_domain.x ? vec3(-solid.x, solid.y, solid.z) :
    ↪ de_domain;
vec3 mandel = solid.x < bubble.x ? solid : bubble;
vec3 result = mandel.x < back.x ? mandel : back;
return result;
250 }

// delta normal calculation

#define DELTANORMAL(DE,E,p) normalize(vec3 \
255    ( DE(p + vec3(E,0.0,0.0)) - DE(p - vec3(E,0.0,0.0)) \
    , DE(p + vec3(0.0,E,0.0)) - DE(p - vec3(0.0,E,0.0)) \
    , DE(p + vec3(0.0,0.0,E)) - DE(p - vec3(0.0,0.0,E)) \
    ))

260 // main entry points

Hit scene(Scene_HIT tag, Random PRNG, Ray V)
{
    // return Union(Light(Sphere(tag, Identity(), V), V, 1.0), SkyBox(tag, Identity ↪
    ↪ (), V));
265    Scene_DE DE;
    vec3 object = V.origin;
    Transform T = Identity();
    float bg = SkyBox(DE, T, V);
    vec3 de = Mandelbrot(object, bg);
270    if (! (de.y > 0.0)) return SkyBox(tag, T, V);
    const float epsilon = 1.0e-3; // FIXME
#define M(p) Mandelbrot(p, SkyBox(DE, T, Ray((p), V.direction, V.wavelength, V. ↪
    ↪ index)))
    vec3 normal = DELTANORMAL(M, epsilon, object);
    // surface
275    Surface S;
    S.position = object;
    S.normal = normal;

```



```

    S.de = de.x;
    vec2 water = Water.nk(V.wavelength);
280 // FIXME the magic numbers to chose materials from DE are annoyance
    if (de.y == 1.0) return Light(S, V, 10.0);
    if (de.y == 2.0) return Glass(PRNG, S, V);
    if (de.y == 3.0) return SoapBubble(PRNG, S, V, 1000.0 * de.z, water);
    if (de.y == 4.0) return Transmit(S, V);
285 return SkyBox(tag, T, V);
}

#if 1

290 // fast
float scene(Scene_DE tag, Random PRNG, Ray V)
{
    return Mandelbrot(V.origin, SkyBox(tag, Identity(), V)).x;
}

295 #else

// slow
float scene(Scene_DE tag, Random PRNG, Ray V)
300 {
    Scene_HIT HIT;
    return scene(HIT, PRNG, V).surface.de;
}

305 #endif

#preset LQ
Exposure = 1
TrigIter = 5
310 TrigLimit = 1.1
FOV = 0.8
Eye = -1.5,-2,-1
Target = -0.75,0,0
Up = 0,0,1
315 Steps = 100
Depth = 3
MinDist = -16
Acne = -12
Aperture = 0.01,0.01
320 Size = 35
Wavelengths = 300,780
Background = ../images/Berlin.equipped.jpg
Distance = 100
Period = 2
325 MinSize = -10
Iterations = 100
Thickness = -10
#endpreset

330 #preset Default
FOV = 1
Eye = -1.5,-2,-1
Target = -0.75,0,0
Up = 0,0,1

```

```

335  Exposure = 1
      TrigIter = 5
      TrigLimit = 1.1
      DebugDepth = false
      DebugNormal = false
340  DebugBounce = false
      Background = ../images/Berlin.equi.jpg
      Distance = 100
      Steps = 100
      Depth = 10
345  MinDist = -16
      Acne = -12
      Aperture = 0.01,0.01
      Size = 35
      Wavelengths = 300,780
350  Period = 12
      MinSize = -10
      Iterations = 100
      Thickness = -10
      #endpreset
355
      #preset Card
      TrigIter = 5
      TrigLimit = 1.10000000000000009
      Exposure = 1
360  FOV = 1
      Eye = -1.5,-2,-1
      Target = -0.75,0,0
      Up = 0,0,1
      DebugDepth = false
365  DebugNormal = false
      DebugBounce = false
      Background = ../images/Grid.equi.png Locked
      Distance = 100
      Steps = 100
370  Depth = 3
      MinDist = -16
      Acne = -12
      Aperture = 0.01,0.021
      Size = 35
375  Wavelengths = 300,780
      Period = 2
      MinSize = -10
      Iterations = 100
      Thickness = -10
380  #endpreset

```

6 examples/SkyBox.frag

```
#version 330 compatibility
```

```
/*
```

```
Raymond - a physics-inspired ray tracer for Fragmentarium
```

```
5 Copyright (C) 2018 Claude Heiland-Allen
```

```
License GPL3+ <http://www.gnu.org/licenses/>
```

```
*/
```

```

#include "Raymond-sRGB.frag"
10  #include "Raymond.frag"

#group Bubble

// average thickness of bubble's soap film in nm
15  uniform float Thickness; slider[0.0,1000.0,10000.0]

// pseudo-random hash
uint hash(uint a)
{
20    return hash_burtle_9(a);
}

Transform Spin;

25  // pinhole camera
Ray camera(Random PRNG, Camera C, vec2 coord, out float intensity)
{
    float t = pi - 2.0 * pi * time / 15.0;
    Spin = Rotate(vec4(Z * sin(t/2.0), cos(t/2.0)));
30    return pinhole(PRNG, C, -coord, pinhole_uniforms(), intensity);
}

// distance estimator raytracer
float raytrace(Random PRNG, Ray V, out Hit h)
35  {
    return raytrace_de(PRNG, V, raytrace_de_uniforms(), h);
}

// CIE observer
40  vec3 film(Random PRNG, float wavelength, float intensity)
{
    return xyz2rgb(observer(wavelength) * intensity);
}

45  // skybox sRGB texture using CRT model
float screen(vec4 tex, float wavelength)
{
    return CRT(sRGB2linear(tex.rgb), wavelength);
}

50  vec4 light(Random PRNG, vec3 from, vec3 dir)
{
    return vec4(0.0);
}

55

// scene definition
#define SCENE(hit,surface,scene_tag) \
hit scene(scene_tag tag, Random PRNG, Ray V) \
60  { \
    return Union \
        ( SkyBox(tag, Spin, V) \
        , SoapBubble \
        ( PRNG \
65    , Sphere(tag, Identity(), V) \

```

```

        , V \
        , Thickness * (1.0 - V.origin.z) \
        , Water_nk(V.wavelength) \
    ) \
70    ); \
}

// scene for DE with lighting
SCENE(Hit, Surface, Scene_HIT)
75

#ifdef DEBUG

// scene for DE only (fast)
SCENE(float, float, Scene_DE)
80

#else

// reuse DE with lighting (slow)
float scene(Scene_DE tag, Random PRNG, Ray V)
85 {
    Scene_HIT HIT;
    return scene(HIT, PRNG, V).surface.de;
}

90 #endif

#preset Default
FOV = 1
95 Eye = 0,2.5,0
Target = 0,0,0
Up = 0,0,1
Exposure = 10
Distance = 100
100 Steps = 100
Depth = 10
MinDist = -16
Acne = -16
Size = 120
105 Aperture = 0.25,1
Wavelengths = 300,780
Thickness = 1000
#endpreset

110 #preset Berlin
Exposure = 1
Background = ../images/Berlin.equipped.jpg
#endpreset

115 #preset Paris
Exposure = 2
Background = ../images/Paris.equipped.jpg
#endpreset

120 #preset Grid
Exposure = 2
Background = ../images/Grid.equipped.png

```

```
#endpreset
```

7 examples/SoapBubble.frag

```
#version 330 compatibility
```

```
/*
Raymond - a physics-inspired ray tracer for Fragmentarium
5 Copyright (C) 2018 Claude Heiland-Allen
License GPL3+ <http://www.gnu.org/licenses/>
*/
```

```
#include "Raymond-sRGB.frag"
```

```
10 #include "Raymond.frag"
```

```
#group Soap
uniform float Thickness; slider[100.0,1000.0,10000.0]
```

```
15 uint hash(uint a)
{
    return hash_burtle_9(a);
}
```

```
20 Ray camera(Random PRNG, Camera C, vec2 coord, out float intensity)
{
    // C.origin.z = 1.0 + 0.5 * sin(2.0 * pi * time / 4.0);
    return pinhole(PRNG, C, -coord, pinhole_uniforms(), intensity);
}
```

```
25 float raytrace(Random PRNG, Ray V, out Hit h)
{
    return raytrace_de(PRNG, V, raytrace_de_uniforms(), h);
}
```

```
30 vec3 film(Random PRNG, float wavelength, float intensity)
{
    return xyz2rgb(observer(wavelength) * intensity);
}
```

```
35 float screen(vec4 tex, float wavelength)
{
    return CRT(sRGB2linear(tex.rgb), wavelength);
}
```

```
40 vec4 light(Random PRNG, vec3 from, vec3 dir)
{
    return vec4(0.0);
}
```

```
45 #define SCENE(hit,surface,scene_tag) \
hit scene(scene_tag tag, Random PRNG, Ray V) \
{ \
50     surface Ground = Plane(tag, Identity(), V, Z, 0.0); \
    return Union3 \
        ( Light(Invert(Sphere(tag, Scale(8.0), V)), V, D65(V.wavelength) * pow(V.ρ \
            ↪ origin.z / 8.0, 16.0) * 32.0) \
```

```

        , SoapBubble(srand(PRNG, 1), Sphere(tag, Translate(vec3(0.0, 0.0, 1.0)), V),
            ↪ V, Thickness * (2.0 - V.origin.z), Water_nk(V.wavelength)) \
    , Checkerboard \
55     ( V.origin \
        , Diffuse(srand(PRNG, 2), Ground, V, 0.5) \
        , Diffuse(srand(PRNG, 2), Ground, V, 0.2) \
        ) \
    ); \
60 }

SCENE(Hit, Surface, Scene_HIT)
#if 1
// fast
65 SCENE(float, float, Scene_DE)
#else
// slow
float scene(Scene_DE tag, Random PRNG, Ray V)
{
70     Scene_HIT HIT;
    return scene(HIT, PRNG, V).surface.de;
}
#endif

75 #preset Default
    Exposure = 1
    FOV = 0.4
    Eye = 0,6,0.25
80    Target = 0,0,1
    Up = 0,0,1
    Steps = 300
    Depth = 10
    Acne = -16
85    Aperture = 0.035
    Size = 35
    Wavelengths = 300,780
#endpreset

```

8 examples/SpongeAndBulb.frag

```

#version 330 compatibility

/*
5  Raymond - a physics-inspired ray tracer for Fragmentarium
   Copyright (C) 2018 Claude Heiland-Allen
   License GPL3+ <http://www.gnu.org/licenses/>
*/

#include "Raymond-sRGB.frag"
10 #include "Raymond.frag"

uniform bool Colour; checkbox[true]

// pseudo-random hash
15 uint hash(uint a)
{
    return hash_burtle_9(a);
}

```

```

}

20 // pinhole camera
Ray camera(Random PRNG, Camera C, vec2 coord, out float intensity)
{
    return pinhole(PRNG, C, -coord, pinhole_uniforms(), intensity);
}

25 // distance estimator raytracer
float raytrace(Random PRNG, Ray V, out Hit h)
{
    return raytrace_de(PRNG, V, raytrace_de_uniforms(), h);
30 }

// CIE observer
vec3 film(Random PRNG, float wavelength, float intensity)
{
35     if (Colour)
        return xyz2rgb(observer(wavelength) * intensity);
    else
        return xyz2rgb(vec3(fp4plus(wavelength) * intensity));
}

40 // sRGB texture using CRT model
float screen(vec4 tex, float wavelength)
{
45     return CRT(sRGB2linear(tex.rgb), wavelength);
}

// scene definition
#define SCENE(hit,surface,scene_tag) \
hit scene(scene_tag tag, Random PRNG, Ray V) \
50 { \
    return Union5 \
        ( Mirror(Invert(Sphere(tag, Scale(8.0), V)), V, Screen_hump(vec3(400.0, ↵
            ↵ 300.0, 1.0), V.wavelength)) \
        , Light(Sphere(tag, Translate(vec3(2.0, 5.5, 5.0)), V), V, 500.0 * D65(V.↵
            ↵ wavelength)) \
        , Diffuse(srand(PRNG, 2), Plane(tag, Identity(), V, Z, 0.0), V, Screen_hump(↵
            ↵ vec3(700.0, 100.0, 1.0), V.wavelength)) \
55     , Diffuse(srand(PRNG, 3), MengerSponge(tag, Translate(vec3(0.0, 0.0, 1.0)), ↵
            ↵ V, 6), V, Screen_hump(vec3(580.0, 200.0, 1.0), V.wavelength)) \
        , Diffuse(srand(PRNG, 4), Mandelbulb(tag, compose(Rotate(vec4(sin(pi/4.0) *↵
            ↵ normalize(vec3(1.0)), cos(pi/4.0))), Translate(vec3(0.0, 0.0, 2.0 + ↵
            ↵ sqrt(8.0)/3.0))), V, 8, 10), V, 1.0) \
        ); \
    }
//     , Light(Plane(tag, Identity(), V, -Z, -6.0), V, 1.0 * D65(V.wavelength)) \
60 vec4 light(Random PRNG, vec3 from, vec3 dir)
{
    vec3 lpos = vec3(2.0, 5.5, 5.0);
    vec3 ldir = lpos - from;
65     float t = cos(asin(1.0 / length(ldir)));
    float s = dot(normalize(ldir), normalize(dir));
    if (length(from) >= 7.999)
    {

```

```

    if (s > t) return vec4(normalize(dir), 1.0); else return vec4(0.0);
70 }
    vec3 to = normalize(gaussian3(srand(PRNG, 5))) + lpos;
    return vec4(normalize(to - from), (1.0 - t) / 2.0);
}

75 // scene for DE with lighting
SCENE(Hit, Surface, Scene_HIT)

#ifndef DEBUG

80 // scene for DE only (fast)
SCENE(float, float, Scene_DE)

#else

85 // reuse DE with lighting (slow)
float scene(Scene_DE tag, Random PRNG, Ray V)
{
    Scene_HIT HIT;
    return scene(HIT, PRNG, V).surface.de;
90 }

#endif

95 #preset Default
    Exposure = 1
    FOV = 1
    Eye = 4,2,4
    Target = 0.5,0,2
100 Up = 0,0,1
    Background =
    Distance = 100
    Steps = 100
    Depth = 10
105 MinDist = -16
    Acne = -12
    Aperture = 0.0,0.0
    Size = 1000
    Wavelengths = 300,780
110 Colour = true
    #endpreset

```

9 .gitignore

-

10 images/berlin.sh

```

#!/bin/sh
# image page: <https://commons.wikimedia.org/wiki/File:Reichstagsufer,_Berlin-↵
    ↵ Mitte,_360x180,_160401,_ako.jpg>
# author: Ansgar Koreng
# license: CC BY-SA 3.0 (DE) <https://creativecommons.org/licenses/by-sa/3.0/de/↵
    ↵ deed.de>

```



```

5  wget -c https://upload.wikimedia.org/wikipedia/commons/7/71/Reichstagsufer%22
    ↳ C_Berlin-Mitte%2C_360x180%2C_160401%2C_ako.jpg
    cp Reichstag*.jpg Berlin.equi.jpg

```

11 images/.gitignore

```

*.exr
*.jpg
*.png

```

12 images/grid.sh

```

#!/bin/sh
# image page: <https://dmswart.com/2016/06/28/drawing-a-panorama/>
# author: D. M. Swart
# license: unknown
5  wget -c https://c2.staticflickr.com/2/1482/26363697850_53505495a2_o_d.png
    cp 26363697850_53505495a2_o_d.png Grid.equi.png

```

13 images/paris.sh

```

#!/bin/sh
# image page: https://commons.wikimedia.org/wiki/File:Paris_s%27%C3%
    ↳ A9veille_equirectangular_panorama.jpg
# author: Alexandre Duret-Lutz <https://www.flickr.com/photos/gadl/456185667/>
# license: CC-BY-SA
5  wget -c https://upload.wikimedia.org/wikipedia/commons/c/c6/Paris_s%27%C3%
    ↳ A9veille_equirectangular_panorama.jpg
    cp Paris_s\'éveille_equirectangular_panorama.jpg Paris.equi.jpg
#convert Paris.equi.jpg Paris.equi.exr
#exrenvmap -c -w 2048 Paris.equi.exr Paris.cube.exr
#convert Paris.cube.exr Paris.cube.png

```

14 include/Raymond-Core.frag

```

#donotrun

/*
Raymond - a physics-inspired ray tracer for Fragmentarium
5  Copyright (C) 2018 Claude Heiland-Allen
    License GPL3+ <http://www.gnu.org/licenses/>
    */

// simple 3D camera, API defined by FragM
10 #camera 3D
    #vertex
    #group Camera
        uniform float FOV; slider[0.0,0.4,2.0] NotLockable
        uniform vec3 Eye; slider[(-50,-50,-50),(0,0,-10),(50,50,50)] NotLockable
15  uniform vec3 Target; slider[(-50,-50,-50),(0,0,0),(50,50,50)] NotLockable
        uniform vec3 Up; slider[(0,0,0),(0,1,0),(0,0,0)] NotLockable

        uniform vec2 pixelSize;

20  varying vec3 Forward;

```

```

varying vec3 UpOrtho;
varying vec3 Right;
varying vec2 coord;
varying vec2 texCoord;
25
void main(void)
{
    Forward = normalize(Target - Eye);
    UpOrtho = normalize(Up - dot(Forward, Up) * Forward);
30    Right = normalize(cross(Forward, UpOrtho));
    coord = (gl_ProjectionMatrix * gl_Vertex).xy;
    coord.x *= pixelSize.y / pixelSize.x;
    texCoord = (gl_Vertex.xy + vec2(1.0)) * 0.5;
    gl_Position = gl_Vertex;
35 }

#endvertex

varying vec3 Forward;
40 varying vec3 UpOrtho;
varying vec3 Right;
varying vec2 coord;
varying vec2 texCoord;

45 uniform float FOV;
uniform vec3 Eye;
uniform vec2 pixelSize;

uniform sampler2D backbuffer;
50 uniform int subframe;
uniform float time;

#group Debug
uniform bool DebugDepth; checkbox[false]
55 uniform bool DebugNormal; checkbox[false]
uniform bool DebugBounce; checkbox[false]

void main(void)
{
60    // seed pseudo-random number generator based on coordinates
    Random PRNG;
    PRNG.seed = hash(vec4(coord, time, subframe));
    PRNG.index = uint(subframe);
    // encapsulate camera parameters from uniform variables
65    Camera C;
    C.origin = Eye;
    C.X = Right;
    C.Y = UpOrtho;
    C.Z = Forward;
70    C.fieldOfView = FOV;
    // render image
    float factor = 1.0;
    Ray V = camera(srand(PRNG, 1), C, coord, factor);
    Hit H;
75    float I = raytrace(srand(PRNG, 2), V, H);
    vec3 rgb = film(srand(PRNG, 3), V.wavelength, I * factor);
    // accumulate linear RGB values

```

```

    vec4 next = vec4(rgb, 1.0);
    if (DebugDepth) next.xyz = vec3(distance(V.origin, H.surface.position));
80  if (DebugNormal) next.xyz = vec3(0.5 + 0.5 * H.surface.normal);
    if (DebugBounce) next.xyz = vec3(0.5 + 0.5 * H.ray.direction);
    if (! (next == next)) next = vec4(0.0); // NaN check
    if (! (dot(next, next) < 1.0/0.0)) next = vec4(0.0); // Infinity check
    vec4 prev = texture(backbuffer, texCoord);
85  gl_FragColor = prev + next;
}

```

15 include/Raymond-D65.frag

```

#donotrun

/*
Raymond - a physics-inspired ray tracer for Fragmentarium
5  Copyright (C) 2018 Claude Heiland-Allen
   License GPL3+ <http://www.gnu.org/licenses/>
*/

// standard illuminant D65
10 float D65(float nm)
   {
   const float d65_min = 300.0;
   const float d65_max = 780.0;
15  const float d65_step = 5.0;
   #define d65_count 97
   const float d65_v[d65_count] = float[d65_count]
   ( 0.034100
    , 1.664300
20  , 3.294500
    , 11.765200
    , 20.236000
    , 28.644700
    , 37.053500
25  , 38.501100
    , 39.948800
    , 42.430200
    , 44.911700
    , 45.775000
30  , 46.638300
    , 49.363700
    , 52.089100
    , 51.032300
    , 49.975500
35  , 52.311800
    , 54.648200
    , 68.701500
    , 82.754900
    , 87.120400
40  , 91.486000
    , 92.458900
    , 93.431800
    , 90.057000
    , 86.682300
45  , 95.773600

```

	, 104.865000
	, 110.936000
	, 117.008000
	, 117.410000
50	, 117.812000
	, 116.336000
	, 114.861000
	, 115.392000
	, 115.923000
55	, 112.367000
	, 108.811000
	, 109.082000
	, 109.354000
	, 108.578000
60	, 107.802000
	, 106.296000
	, 104.790000
	, 106.239000
	, 107.689000
65	, 106.047000
	, 104.405000
	, 104.225000
	, 104.046000
	, 102.023000
70	, 100.000000
	, 98.167100
	, 96.334200
	, 96.061100
	, 95.788000
75	, 92.236800
	, 88.685600
	, 89.345900
	, 90.006200
	, 89.802600
80	, 89.599100
	, 88.648900
	, 87.698700
	, 85.493600
	, 83.288600
85	, 83.493900
	, 83.699200
	, 81.863000
	, 80.026800
	, 80.120700
90	, 80.214600
	, 81.246200
	, 82.277800
	, 80.281000
	, 78.284200
95	, 74.002700
	, 69.721300
	, 70.665200
	, 71.609100
	, 72.979000
100	, 74.349000
	, 67.976500
	, 61.604000

```

    , 65.744800
    , 69.885600
105  , 72.486300
    , 75.087000
    , 69.339800
    , 63.592700
    , 55.005400
110  , 46.418200
    , 56.611800
    , 66.805400
    , 65.094100
    , 63.382800
115 );
    float f = (nm - d65_min) / d65_step;
    int i0 = int(floor(f));
    int i1 = i0 + 1;
    float f1 = f - float(i0);
120  if (i0 < 0) return 0.0;
    if (i1 > d65_count - 1) return 0.0;
    return mix(d65_v[i0], d65_v[i1], f1) * 0.01;
#undef d65_count
}

```

16 include/Raymond-Defs.frag

```

#ifndef raymond
#define raymond

/*
Raymond - a physics-inspired ray tracer for Fragmentarium
5  Copyright (C) 2018 Claude Heiland-Allen
   License GPL3+ <http://www.gnu.org/licenses/>
*/

struct Random { uint seed, index; };
10 struct Camera { vec3 origin, X, Y, Z; float fieldOfView; };
struct Ray { vec3 origin, direction; float wavelength; vec2 index; };
struct Surface { vec3 position; vec3 normal; float de; };
struct Hit { Surface surface; Ray ray; float factor; float emit; };

15 // implement these
uint hash(uint n);
Ray camera(Random PRNG, Camera C, vec2 coord, out float intensity);
float /* intensity */ raytrace(Random PRNG, Ray V, out Hit h);
vec3 /* linear RGB */ film(Random PRNG, float wavelength, float intensity);
20 vec4 /* direction, weight */ light(Random PRNG, vec3 from, vec3 dir);

// perturb a random number generator
Random srand(Random PRNG, int seed)
{
25  PRNG.seed = hash(vec2(hash(PRNG.seed), hash(uint(seed))));
  return PRNG;
}

// scene definition
30 struct Scene.DE { int dummy; };
struct Scene.HIT { int dummy; };

```

```

float scene(Scene_DE tag, Random PRNG, Ray V);
35 Hit scene(Scene_HIT tag, Random PRNG, Ray V);

```

17 include/Raymond-FP4Plus.frag

```

#donotrun

/*
Raymond - a physics-inspired ray tracer for Fragmentarium
5 Copyright (C) 2018 Claude Heiland-Allen
License GPL3+ <http://www.gnu.org/licenses/>
*/

// Ilford FP4 Plus black and white film
10 float fp4plus(float wavelength)
{
const int fp4plus_u[350] = int[350]
15 ( 0x00, 0x00, 0x00, 0x00, 0x00, 0x00, 0x00, 0x00, 0x00, 0x00, 0x00, 0x00,
, 0x00, 0x00, 0x00, 0x00, 0x0d, 0x22, 0x35, 0x42, 0x4f, 0x5a
, 0x62, 0x68, 0x6d, 0x71, 0x75, 0x78, 0x7c, 0x7f, 0x81, 0x83
, 0x86, 0x87, 0x89, 0x8b, 0x8d, 0x8f, 0x91, 0x94, 0x95, 0x98
, 0x9b, 0x9c, 0x9f, 0xa1, 0xa3, 0xa5, 0xa7, 0xa9, 0xab, 0xac
, 0xad, 0xaf, 0xb0, 0xb1, 0xb2, 0xb3, 0xb4, 0xb4, 0xb5, 0xb5
20 , 0xb6, 0xb6, 0xb6, 0xb7, 0xb7, 0xb7, 0xb8, 0xb8, 0xb9, 0xb9
, 0xba, 0xbb, 0xbb, 0xbc, 0xbd, 0xbd, 0xbe, 0xbe, 0xc0, 0xc0
, 0xc2, 0xc2, 0xc3, 0xc4, 0xc5, 0xc6, 0xc7, 0xc8, 0xca, 0xcb
, 0xcc, 0xcd, 0xce, 0xcf, 0xd0, 0xd1, 0xd2, 0xd2, 0xd3, 0xd4
, 0xd4, 0xd5, 0xd5, 0xd6, 0xd6, 0xd7, 0xd7, 0xd7, 0xd8, 0xd8
25 , 0xd8, 0xd8, 0xd9, 0xd9, 0xda, 0xda, 0xda, 0xda, 0xda, 0xda
, 0xda, 0xda, 0xda, 0xda, 0xda, 0xda, 0xda, 0xda, 0xda, 0xda
, 0xda, 0xda, 0xda, 0xda, 0xda, 0xda, 0xda, 0xd9, 0xd9, 0xd9
, 0xd9, 0xd8, 0xd8, 0xd8, 0xd8, 0xd7, 0xd7, 0xd7, 0xd7, 0xd6
, 0xd6, 0xd6, 0xd6, 0xd5, 0xd5, 0xd5, 0xd5, 0xd5, 0xd5, 0xd5
30 , 0xd6, 0xd6, 0xd6, 0xd7, 0xd7, 0xd8, 0xd8, 0xda, 0xda, 0xdb
, 0xdc, 0xdd, 0xde, 0xde, 0xdf, 0xe0, 0xe0, 0xe0, 0xe1, 0xe2
, 0xe2, 0xe2, 0xe3, 0xe3, 0xe3, 0xe3, 0xe3, 0xe3, 0xe3, 0xe3
, 0xe3, 0xe3, 0xe3, 0xe3, 0xe2, 0xe2, 0xe3, 0xe3, 0xe3, 0xe3
, 0xe3, 0xe4, 0xe4, 0xe5, 0xe6, 0xe6, 0xe7, 0xe7, 0xe8, 0xe9
35 , 0xe9, 0xea, 0xea, 0xeb, 0xec, 0xec, 0xec, 0xed, 0xee, 0xee, 0xef
, 0xef, 0xf0, 0xf1, 0xf1, 0xf2, 0xf3, 0xf4, 0xf5, 0xf5, 0xf6
, 0xf6, 0xf7, 0xf8, 0xf8, 0xf9, 0xf9, 0xfa, 0xfa, 0xfb, 0xfb
, 0xfb, 0xfc, 0xfc, 0xfc, 0xfc, 0xfd, 0xfd, 0xfd, 0xfe, 0xfe
, 0xfe, 0xfe, 0xfe, 0xfe, 0xfe, 0xfe, 0xfe, 0xfe, 0xfe, 0xfe
40 , 0xfd, 0xfd, 0xfd, 0xfc, 0xfc, 0xfb, 0xfb, 0xfb, 0xfa, 0xfa
, 0xfa, 0xfa, 0xfa, 0xfa, 0xfa, 0xfa, 0xfa, 0xfa, 0xfa, 0xfa
, 0xfa, 0xf9, 0xf8, 0xf6, 0xf4, 0xf1, 0xee, 0xeb, 0xe8, 0xe5
, 0xe2, 0xde, 0xdb, 0xd7, 0xd3, 0xcf, 0xcb, 0xc7, 0xc2, 0xbd
, 0xb8, 0xb2, 0xad, 0xa7, 0xa1, 0x9b, 0x94, 0x8c, 0x84, 0x7c
45 , 0x72, 0x68, 0x5c, 0x4f, 0x3d, 0x2e, 0x1c, 0x0d, 0x00, 0x00
, 0x00, 0x00, 0x00, 0x00, 0x00, 0x00, 0x00, 0x00, 0x00, 0x00
, 0x00, 0x00, 0x00, 0x00, 0x00, 0x00, 0x00, 0x00, 0x00, 0x00
, 0x00, 0x00, 0x00, 0x00, 0x00, 0x00, 0x00, 0x00, 0x00, 0x00
);
50 float f = wavelength - 350.0;
int i0 = int(floor(f));

```

```

    int i1 = i0 + 1;
    float f1 = f - float(i0);
    if (i0 < 0) return 0.0;
55    if (i1 > 350 - 1) return 0.0;
    return mix(float(fp4plus_u[i0]), float(fp4plus_u[i1]), f1) / float(0xfe);
}

```

18 include/Raymond-Fractal.frag

```

#donotrun

/*
Raymond - a physics-inspired ray tracer for Fragmentarium
5  Copyright (C) 2018 Claude Heiland-Allen
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*/

#if 0
10 #define MengerSponge_(type) \
MengerSponge(type tag, Transform T, Ray V, int depth) \
{ \
    vec3 p = backwardP(T, V.origin); \
15    vec3 q0 = vec3(0.0); \
    float r = 1.5; \
    for (int i = 0; i < depth; ++i) \
    { \
        vec3 q1 = vec3(0.0); \
20        float d = 1.0 / 0.0; \
        for (int x = -1; x <= 1; ++x) \
        for (int y = -1; y <= 1; ++y) \
        for (int z = -1; z <= 1; ++z) \
        { \
25            if (int(x == 0) + int(y == 0) + int(z == 0) > 1) continue; \
            vec3 q = q0 + vec3(x, y, z) / r; \
            float de = length(p - q); \
            if (de < d) { d = de; q1 = q; } \
        } \
30        q0 = q1; \
        r *= 3.0; \
    } \
    return Cube(tag, compose(Translate(q0), T), V, 1.5 / r); \
}
35 float MengerSponge_(Scene.DE)

Surface MengerSponge_(Scene.HIT)
#undef MengerSponge_
40 #endif

// delta normal calculation
#define DELTANORMAL(DE,E,p) normalize(vec3 \
45    ( DE(p + vec3(E,0.0,0.0)) - DE(p - vec3(E,0.0,0.0)) \
    , DE(p + vec3(0.0,E,0.0)) - DE(p - vec3(0.0,E,0.0)) \
    , DE(p + vec3(0.0,0.0,E)) - DE(p - vec3(0.0,0.0,E)) \
    ))

```

```

50 float MengerSponge(Scene.DE tag, Transform T, Ray V, int depth)
{
    const float Scale = 3.0;
    const vec3 Offset = vec3(1.0);
    vec3 z = backwardP(T, V.origin);
55     int n = 0;
    while (n < depth) {
        z = abs(z);
        if (z.x < z.y) { z.xy = z.yx; }
        if (z.x < z.z) { z.xz = z.zx; }
60     if (z.y < z.z) { z.yz = z.zy; }
        z = Scale*z-Offset*(Scale-1.0);
        if ( z.z < -0.5*Offset.z*(Scale-1.0) ) z.z += Offset.z*(Scale-1.0);
        n++;
    }
65     vec3 d = abs(z) - vec3(1.0);
    float de = length(max(d, 0.0)) + min(max(d.x, max(d.y, d.z)), 0.0);
    return forwardD(T, de * pow(Scale, float(-n)));
}

70 Surface MengerSponge(Scene.HIT tag, Transform T, Ray V, int depth)
{
    Scene.DE DE;
    float de = MengerSponge(DE, T, V, depth);
    const float epsilon = 1.0e-3; // FIXME
75 #define M(p) MengerSponge(DE, T, Ray((p), V.direction, V.wavelength, V.index), ↵
    ↵ depth)
    vec3 normal = DELTANORMAL(M, epsilon, V.origin);
#undef M
    // surface
    return Surface(V.origin, normal, de);
80 }

float Mandelbulb(Scene.DE tag, Transform T, Ray V, int Power, int depth)
{
    vec3 pos = backwardP(T, V.origin);
85     vec3 z = pos;
    const float Bailout = 25.0;
    float dr = 1.0;
    float r = length(z);
    int n = 0;
90     while (n < depth && r < Bailout) {
        // This is a power function taken from the implementation by Enforcer:
        // http://www.fractalforums.com/mandelbulb-implementation/realtime-↵
        ↵ renderingoptimisations/
        //
        // I cannot follow its derivation from spherical coordinates,
95     // but it does give a nice mandelbrot like object for Power=2
        // z=abs(z);
        //void powN2(inout vec3 z, float zr0, inout float dr, float Power) {
100     float zr0 = r;
        float zo0 = asin( z.z/zr0 );
        float zi0 = atan( z.y,z.x );
        float zr = pow( zr0, Power-1.0 );
        float zo = zo0 * Power;
        float zi = zi0 * Power;
    }
}

```



```

105      // mermelada's tweak
      // http://www.fractalforums.com/new-theories-and-research/error-↵
      ↵ estimation-of-distance-estimators/msg102670/?topicseen#msg102670
      const float DerivativeBias = 1.0;
      dr = max(dr*DerivativeBias, zr*dr*Power + 1.0);
      zr *= zr0;
      z = zr*vec3( cos(z0)*cos(zi), cos(z0)*sin(zi), sin(z0) );
110  //}
      z += pos;
      r = length(z);
      n++;
    }
115    float de = 0.5*log(r)*r/dr;
    return forwardD(T, de);
  }

Surface Mandelbulb(Scene_HIT tag, Transform T, Ray V, int power, int depth)
120 {
    Scene_DE DE;
    float de = Mandelbulb(DE, T, V, power, depth);
    const float epsilon = 1.0e-5; // FIXME
    #define M(p) Mandelbulb(DE, T, Ray((p), V.direction, V.wavelength, V.index), ↵
      ↵ power, depth)
125    vec3 normal = DELTANORMAL(M, epsilon, V.origin);
    #undef M
    // surface
    return Surface(V.origin, normal, de);
  }
130 #undef DELTANORMAL

```

19 include/Raymond.frag

```

#donotrun
#info Raymond - a physics-inspired ray tracer (C) 2018 Claude Heiland-Allen (↵
  ↵ License GPL3+)

/*
5  Raymond - a physics-inspired ray tracer for Fragmentarium
  Copyright (C) 2018 Claude Heiland-Allen
  License GPL3+ <http://www.gnu.org/licenses/>
  */

10  const float pi = 3.141592653589793;
  const vec3 X = vec3(1.0, 0.0, 0.0);
  const vec3 Y = vec3(0.0, 1.0, 0.0);
  const vec3 Z = vec3(0.0, 0.0, 1.0);

15  #include "Complex.frag"

  #include "Raymond-Hash.frag"
  #include "Raymond-Defs.frag"
  #ifndef RaymondNoMain
20  #include "Raymond-Core.frag"
  #endif
  #include "Raymond-Random.frag"
  #include "Raymond-Halton.frag"

```

```

#include "Raymond-Quaternion.frag"
25 #include "Raymond-Transform.frag"
#include "Raymond-Surface.frag"
#include "Raymond-Fractal.frag"
#include "Raymond-Material.frag"
#include "Raymond-D65.frag"
30 #include "Raymond-Glass.frag"
#include "Raymond-Quartz.frag"
#include "Raymond-Water.frag"
#include "Raymond-Observer.frag"
#include "Raymond-FP4Plus.frag"
35 #include "Raymond-Screen.frag"
#include "Raymond-SkyBox.frag"
#include "Raymond-Trace.frag"
#include "Raymond-Pinhole.frag"

```

20 include/Raymond-Glass.frag

```

#donotrun

/*
Raymond - a physics-inspired ray tracer for Fragmentarium
5 Copyright (C) 2018 Claude Heiland-Allen
License GPL3+ <http://www.gnu.org/licenses/>
*/

// database/glass/schott/F2.yml
10 float Glass_n(float wavelength) {
    float l2 = 1.0e-6 * wavelength * wavelength;
    return sqrt(1.0 + l2 *
15      ( 1.34533359 / (l2 - 0.00997743871)
        + 0.209073176 / (l2 - 0.0470450767)
        + 0.937357162 / (l2 - 111.886764)
      ));
}

20 float Glass_k(float wavelength) {
    const vec2 glass_lk[13] = vec2[13]
      ( vec2(1000.0 * 0.390, 2.8886e-8)
        , vec2(1000.0 * 0.400, 1.9243e-8)
        , vec2(1000.0 * 0.405, 1.6869e-8)
25      , vec2(1000.0 * 0.420, 1.2087e-8)
        , vec2(1000.0 * 0.436, 9.7490e-9)
        , vec2(1000.0 * 0.460, 8.8118e-9)
        , vec2(1000.0 * 0.500, 4.7818e-9)
        , vec2(1000.0 * 0.546, 3.4794e-9)
30      , vec2(1000.0 * 0.580, 3.6961e-9)
        , vec2(1000.0 * 0.620, 3.9510e-9)
        , vec2(1000.0 * 0.660, 6.3120e-9)
        , vec2(1000.0 * 0.700, 4.4608e-9)
        , vec2(1000.0 * 1.060, 6.7549e-9)
35      );
    if (wavelength < glass_lk[0][0]) return glass_lk[0][1];
    for (int i0 = 0; i0 < 12; ++i0) {
        int i1 = i0 + 1;
        float l0 = glass_lk[i0][0];

```

```

40     float l1 = glass_lk[i1][0];
        if (10 <= wavelength && wavelength <= 11) {
            float f1 = (wavelength - 10) / (11 - 10);
            float k0 = glass_lk[i0][1];
            float k1 = glass_lk[i1][1];
45     return mix(k0, k1, f1);
        }
    }
    return glass_lk[12][1];
}

50 vec2 Glass_nk(float wavelength)
{
    return vec2(Glass_n(wavelength), Glass_k(wavelength));
}

55 float Glass(Random PRNG, float S, Ray V)
{
    return S;
}

60 Hit Glass(Random PRNG, Surface S, Ray V)
{
    return Transparent(PRNG, S, V, Glass_nk(V.wavelength));
}

```

21 include/Raymond-Halton.frag

```

#donotrun

/*
Raymond - a physics-inspired ray tracer for Fragmentarium
5 Copyright (C) 2018 Claude Heiland-Allen
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*/

// https://en.wikipedia.org/wiki/Halton_sequence

10 float halton(uint b, uint i)
{
    float f = 1.0;
    float r = 0.0;
15     if (b > 1u)
        while (i > 0u)
        {
            f /= float(b);
            r += f * float(i % b);
20         i /= b;
        }
    return r;
}

25 vec2 halton(ivec2 b, uint i)
{
    return vec2(halton(b.x, i), halton(b.y, i));
}

```

```

30  vec3 halton(uvec3 b, uint i)
    {
        return vec3(halton(b.x, i), halton(b.y, i), halton(b.z, i));
    }

35  vec4 halton(uvec4 b, uint i)
    {
        return vec4(halton(b.x, i), halton(b.y, i), halton(b.z, i), halton(b.w, i));
    }

40  float halton(Random PRNG, int b1)
    {
        float h = halton(uint(b1), PRNG.index) + uniform1(PRNG);
        return h - floor(h);
    }

45  vec2 halton(Random PRNG, int b1, int b2)
    {
        float theta = 2.0 * pi * uniform1(srand(PRNG, 1));
        float c = cos(theta);
50  float s = sin(theta);
        float r = 1.0 / (abs(c) + abs(s));
        mat2 m = mat2(c, s, -s, c) / r;
        vec2 h = m * halton(uvec2(b1, b2), PRNG.index) + uniform2(srand(PRNG, 2));
        return h - floor(h);
55  }

    vec3 halton(Random PRNG, int b1, int b2, int b3)
    {
        vec3 h = halton(uvec3(b1, b2, b3), PRNG.index) + uniform3(PRNG);
60  return h - floor(h);
    }

    vec4 halton(Random PRNG, int b1, int b2, int b3, int b4)
    {
65  vec4 h = halton(uvec4(b1, b2, b3, b4), PRNG.index) + uniform4(PRNG);
        return h - floor(h);
    }

    float halton1(Random PRNG) { return halton(PRNG, 2); }
70  vec2 halton2(Random PRNG) { return halton(PRNG, 2, 3); }
    vec3 halton3(Random PRNG) { return halton(PRNG, 2, 3, 5); }
    vec4 halton4(Random PRNG) { return halton(PRNG, 2, 3, 5, 7); }

    vec2 haltonDisc(Random PRNG)
75  {
        return uniformDisc(halton2(PRNG));
    }

```

22 include/Raymond-Hash.frag

```
#donotrun
```

```
/*
```

```
Raymond - a physics-inspired ray tracer for Fragmentarium
```

```
5  Copyright (C) 2018 Claude Heiland-Allen
```

```
License GPL3+ <http://www.gnu.org/licenses/>
```

```

*/
// implement this
10  uint hash(uint a);

// scaling from uint to [0,1)
15  float uniform01(uint a) { return float(a) / 4294967296.0; }

// hashes of other/larger objects

uint hash(int a) { return hash(uint(a)); }
20  uint hash(float a) { return hash(floatBitsToUint(a)); }
uint hash(uvec2 a) { return hash(a.x ^ hash(a.y)); }
uint hash(uvec3 a) { return hash(a.x ^ hash(a.yz)); }
uint hash(uvec4 a) { return hash(a.x ^ hash(a.yzw)); }
uint hash(ivec2 a) { return hash(uint(a.x) ^ hash(a.y)); }
25  uint hash(ivec3 a) { return hash(uint(a.x) ^ hash(a.yz)); }
uint hash(ivec4 a) { return hash(uint(a.x) ^ hash(a.yzw)); }
uint hash(vec2 a) { return hash(floatBitsToUint(a.x) ^ hash(a.y)); }
uint hash(vec3 a) { return hash(floatBitsToUint(a.x) ^ hash(a.yz)); }
uint hash(vec4 a) { return hash(floatBitsToUint(a.x) ^ hash(a.yzw)); }
30

// http://www.burtleburtle.net/bob/hash/integer.html

uint hash_burtle_1(uint a)
{
35  a = (a ^ 61u) ^ (a >> 16u);
a = a + (a << 3u);
a = a ^ (a >> 4u);
a = a * 0x27d4eb2du;
a = a ^ (a >> 15u);
40  return a;
}

uint hash_burtle_2(uint a)
{
45  a = (a+0x7ed55d16u) + (a<<12u);
a = (a^0xc761c23cu) ^ (a>>19u);
a = (a+0x165667b1u) + (a<<5u);
a = (a+0xd3a2646cu) ^ (a<<9u);
a = (a+0xfd7046c5u) + (a<<3u);
50  a = (a^0xb55a4f09u) ^ (a>>16u);
return a;
}

uint hash_burtle_3(uint a)
55  {
a -= (a<<6u);
a ^= (a>>17u);
a -= (a<<9u);
a ^= (a<<4u);
60  a -= (a<<3u);
a ^= (a<<10u);
a ^= (a>>15u);
return a;
}

```

```

}
65  uint hash_burtle_4(uint a)
    {
        a += ~(a<<15u);
        a ^=  (a>>10u);
70  a +=  (a<<3u);
        a ^=  (a>>6u);
        a += ~(a<<11u);
        a ^=  (a>>16u);
        return a;
75  }

uint hash_burtle_5(uint a)
{
    a = (a+0x479ab41du) + (a<<8u);
80  a = (a^0xe4aa10ceu) ^ (a>>5u);
    a = (a+0x9942f0a6u) - (a<<14u);
    a = (a^0x5aedd67du) ^ (a>>3u);
    a = (a+0x17bea992u) + (a<<7u);
    return a;
85  }

uint hash_burtle_6(uint a)
{
    a = (a^0xdeadbeefu) + (a<<4u);
90  a = a ^ (a>>10u);
    a = a + (a<<7u);
    a = a ^ (a>>13u);
    return a;
}
95  uint hash_burtle_7(uint a)
    {
        a = a ^ (a>>4u);
        a = (a^0xdeadbeefu) + (a<<5u);
100 a = a ^ (a>>11u);
        return a;
    }

uint hash_burtle_8(uint a)
105 {
    a = (a+0x479ab41du) + (a<<8u);
    a = (a^0xe4aa10ceu) ^ (a>>5u);
    a = (a+0x9942f0a6u) - (a<<14u);
    a = (a^0x5aedd67du) ^ (a>>3u);
110 a = (a+0x17bea992u) + (a<<7u);
    return a;
}

uint hash_burtle_9(uint a)
115 {
    a = (a+0x7ed55d16u) + (a<<12u);
    a = (a^0xc761c23cu) ^ (a>>19u);
    a = (a+0x165667b1u) + (a<<5u);
    a = (a+0xd3a2646cu) ^ (a<<9u);
120 a = (a+0xfd7046c5u) + (a<<3u);

```

```

    a = (a^0xb55a4f09u) ^ (a>>16u);
    return a;
}

125 uint hash_burtle_10(uint a)
{
    a = (a+0x7fb9b1eeu) + (a<<12u);
    a = (a^0xab35dd63u) ^ (a>>19u);
    a = (a+0x41ed960du) + (a<<5u);
130 a = (a+0xc7d0125eu) ^ (a<<9u);
    a = (a+0x071f9f8fu) + (a<<3u);
    a = (a^0x55ab55b9u) ^ (a>>16u);
    return a;
}

135 uint hash_burtle_11(uint a)
{
    a -= (a<<6u);
    a ^= (a>>17u);
140 a -= (a<<9u);
    a ^= (a<<4u);
    a -= (a<<3u);
    a ^= (a<<10u);
    a ^= (a>>15u);
145 return a;
}

uint hash_burtle_12(uint a)
{
150 a += ~(a<<15u);
    a ^= (a>>10u);
    a += (a<<3u);
    a ^= (a>>6u);
    a += ~(a<<11u);
155 a ^= (a>>16u);
    return a;
}

```

23 include/Raymond-Lettuce.frag

```

#donotrun

/*
Raymond - a physics-inspired ray tracer for Fragmentarium
5 Copyright (C) 2018,2019 Claude Heiland-Allen
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Lettuce: <https://fractalforums.org/f/28/t/2996/msg16077#msg16077>
*/

10 #define DELTA(N,E,p) vec3 \
    ( N(p + vec3(E,0.0,0.0)) - N(p - vec3(E,0.0,0.0)) \
      , N(p + vec3(0.0,E,0.0)) - N(p - vec3(0.0,E,0.0)) \
      , N(p + vec3(0.0,0.0,E)) - N(p - vec3(0.0,0.0,E)) \
15 )

float Lettuce(vec3 p, int maxiter)

```

```

{
    float a = p.x;
20    float b = p.y;
    float c = p.z;
    float len2 = dot(p, p);
    float rlen;
    int i = 0;
25    while ((len2 < 16.0) && (i < maxiter)) {
        i++;
        rlen = 1.0/sqrt(len2);
        p *= rlen; // normalize vector to unit length => project onto sphere
        // find X-related iso-plane: polar projection onto unit circle
30        float Kx = 2.0*p.x*(1.0 - p.y)/((p.y - 2.0)*p.y + p.x*p.x + 1.0);
        float Ky = 1.0 - 2.0*((p.y - 2.0)*p.y + 1.0) /
            ((p.y - 2.0)*p.y + p.x*p.x + 1.0);
        // doubled point
        float K2x = -2.0*Kx*Ky;
35        float K2y = -(Ky*Ky - Kx*Kx);
        // two more doublings (for total power eight)
        Kx = -2.0*K2x*K2y;
        Ky = -(K2y*K2y - K2x*K2x);
        K2x = -2.0*Kx*Ky;
40        K2y = -(Ky*Ky - Kx*Kx);
        // (relevant) normal vector coordinates of doubled point plane
        float nlx = K2y - 1.0;
        float nly = -K2x;
        // find Z-related iso-plane: polar projection onto unit circle
45        float Kz = 2.0*p.z*(1.0 - p.y)/((p.y - 2.0)*p.y + p.z*p.z + 1.0);
        Ky = 1.0 - 2.0*((p.y - 2.0)*p.y + 1.0)/((p.y - 2.0)*p.y + p.z*p.z + 1.0);
        // doubled point
        float K2z = -2.0*Kz*Ky;
        K2y = -(Ky*Ky - Kz*Kz);
50        // two more doublings (for total power eight)
        Kz = -2.0*K2z*K2y;
        Ky = -(K2y*K2y - K2z*K2z);
        K2z = -2.0*Kz*Ky;
        K2y = -(Ky*Ky - Kz*Kz);
55        // (relevant) normal vector coordinates of doubled point plane
        float n2y = -K2z;
        float n2z = K2y - 1.0;
        // compute position of doubled point as intersection of planes and sphere
        // solved ray parameter
60        float nt = 2.0*(nlx*nlx*n2z*n2z)/((nlx*nlx + nly*nly)*n2z*n2z
            + nlx*nlx*n2y*n2y);
        // doubled point position
        p.y = 1.0 - nt;
        p.x = nly*(1.0 - p.y)/nlx;
65        p.z = n2y*(1.0 - p.y)/n2z;
        // raise original length to the power, then add constant
        // p *= len2;
        p *= len2*len2*len2*len2; // for 8th power
        p += vec3(a,b,c);
70        len2 = dot(p, p);
    }
    if (len2 < 16.0) {
        return float(maxiter);
    }
}

```



```

75     return float(i) + 1.0 - log(sqrt(len2)) / log(8.0);
    }

    float Lettuce(Scene_DE tag, Transform T, Ray V, int maxiter)
    {
80     vec3 origin = backwardP(T, V.origin);
        const float epsilon = 1.0e-4; // FIXME
#define M(p) Lettuce(p, maxiter)
        vec3 gradient = DELTA(M, epsilon, origin) / (2.0 * epsilon);
#undef M
85     float de = 0.25 * 1.0 / (log(8.0) * length(gradient));
        return forwardD(T, de);
    }

    Surface Lettuce(Scene_HIT tag, Transform T, Ray V, int maxiter)
90    {
        vec3 origin = backwardP(T, V.origin);
        const float epsilon = 1.0e-4; // FIXME
#define M(p) Lettuce(p, maxiter)
        vec3 gradient = DELTA(M, epsilon, origin) / (2.0 * epsilon);
95    #undef M
        float de = 0.25 * 1.0 / (log(8.0) * length(gradient));
        vec3 normal = normalize(-gradient); // FIXME normal of escape field, not of ↯
            ↵ distance?
        // surface
        return Surface(forwardP(T, origin), forwardN(T, normal), forwardD(T, de));
100    }

    #undef DELTA

```

24 include/Raymond-Material.frag

```

#donotrun

/*
Raymond - a physics-inspired ray tracer for Fragmentarium
5  Copyright (C) 2018 Claude Heiland-Allen
    License GPL3+ <http://www.gnu.org/licenses/>
*/

// CSG union: minimum by de
10 Hit Union(in Hit a)
    {
        return a;
    }

15 Hit Union(in Hit a, in Hit b)
    {
        if (a.surface.de < b.surface.de) return a; else return b;
    }

20 Hit Union(in Hit a, in Hit b, in Hit c)
    {
        return Union(Union(a, b), c);
    }

25

```

```

Hit Union(in Hit a, in Hit b, in Hit c, in Hit d)
{
    return Union(Union(Union(a, b), c), d);
}
30 Hit Union(in Hit a, in Hit b, in Hit c, in Hit d, in Hit e)
{
    return Union(Union(Union(Union(a, b), c), d), e);
}
35 Hit Union(in Hit a, in Hit b, in Hit c, in Hit d, in Hit e, in Hit f)
{
    return Union(Union(Union(Union(Union(a, b), c), d), e), f);
}
40 Hit Union(in Hit a, in Hit b, in Hit c, in Hit d, in Hit e, in Hit f, in Hit g)
{
    return Union(Union(Union(Union(Union(Union(a, b), c), d), e), f), g);
}
45 // CSG intersection: maximum by de

Hit Intersection(in Hit a, in Hit b)
{
50     if (a.surface.de > b.surface.de) return a; else return b;
}

Hit Intersection(in Hit a, in Hit b, in Hit c)
{
55     return Intersection(Intersection(a, b), c);
}

Hit Intersection(in Hit a, in Hit b, in Hit c, in Hit d)
{
60     return Intersection(Intersection(Intersection(a, b), c), d);
}

Hit Intersection(in Hit a, in Hit b, in Hit c, in Hit d, in Hit e)
{
65     return Intersection(Intersection(Intersection(Intersection(a, b), c), d), e);
}

Hit Intersection(in Hit a, in Hit b, in Hit c, in Hit d, in Hit e, in Hit f)
{
70     return Intersection(Intersection(Intersection(Intersection(Intersection(a, b), ↵
        ↵ c), d), e), f);
}

// virtual surface (transmits everything)

75 float Transmit(float S, Ray V)
{
    return S;
}

80 Hit Transmit(Surface S, Ray V)
{

```

```

    V.origin = S.position;
    Hit h;
    h.surface = S;
85    h.ray = V;
    h.factor = 1.0;
    h.emit = 0.0;
    return h;
}
90 // opaque emissive material

float Light(float S, Ray V, float brightness)
{
95    return S;
}

Hit Light(Surface S, Ray V, float brightness)
{
100    V.origin = S.position;
    V.direction = vec3(0.0);
    Hit h;
    h.surface = S;
    h.ray = V;
105    h.factor = 0.0;
    h.emit = brightness;//S.de < 1.0e-4 ? brightness : 0.0;
    return h;
}

110 // perfectly reflective material

float Mirror(float S, Ray V, float albedo)
{
    return S;
115 }

Hit Mirror(Surface S, Ray V, float albedo)
{
    V.origin = S.position;
120    V.direction = reflect(V.direction, S.normal);
    return Hit(S, V, albedo, 0.0);
}

// opaque diffuse material
125 float Diffuse(Random PRNG, float S, Ray V, float albedo)
{
    return S;
}

130 Hit Diffuse(Random PRNG, Surface S, Ray V, float albedo)
{
    V.origin = S.position;
    V.direction = cosHemisphere(haltonDisc(PRNG), S.normal);
135    Hit h;
    h.surface = S;
    h.ray = V;
    h.emit = 0.0;

```

```

    h.factor = albedo / pi;
140    return h;
}

// opaque glossy material

145 float CookTorrance(vec3 I, vec3 O, vec3 N, float albedo, float shine, float ↵
    ↵ roughness, float eta)
{
    float diffuse = albedo / pi;
    vec3 H = normalize(O + I); // half vector
    float a2 = roughness * roughness;
150    // distribution term (microfacets)
    float D = 0.0;
    float HN = dot(H, N);
    if (HN > 0.0)
    {
155        float HN2 = HN * HN;
        float den = HN2 * a2 + (1.0 - HN2);
        D = a2 / (pi * den * den);
    }
    // fresnel term (approximation)
160    float e = (eta - 1.0) / (eta + 1.0);
    float F = mix(pow(1.0 - dot(H, O), 5.0), 1.0, e * e);
    // geometry term (self-occlusion)
    float G = 1.0;
    float IH = dot(I, H);
165    float OH = dot(O, H);
    if ((dot(I, N) > 0.0) == (IH > 0.0)) G *= 2.0 / (1.0 + sqrt(1.0 + a2 * (1.0 - ↵
        ↵ IH * IH) / (IH * IH)));
    if ((dot(O, N) > 0.0) == (OH > 0.0)) G *= 2.0 / (1.0 + sqrt(1.0 + a2 * (1.0 - ↵
        ↵ OH * OH) / (OH * OH)));
    // combined
    float specular = D * F * G / (4.0 * dot(I, N) * dot(O, N));
170    // surface
    return mix(diffuse, specular, shine);
}

float CookTorrance(Random PRNG, float S, Ray V, float albedo, float shine, float ↵
    ↵ roughness, vec2 index)
175 {
    return S;
}

Hit CookTorrance(Random PRNG, Surface S, Ray I, float albedo, float shine, float ↵
    ↵ roughness, vec2 index)
180 {
    Ray O = I;
    O.origin = S.position;
    O.direction = cosHemisphere(haltonDisc(PRNG), S.normal);
    float eta = I.index.x / index.x;
185    Hit h;
    h.surface = S;
    h.ray = O;
    h.emit = 0.0;
    h.factor = CookTorrance(I.direction, O.direction, S.normal, albedo, shine, ↵
        ↵ roughness, eta);
}

```

```

190     return h;
    }

    // Fresnel equations

195 struct Fresnel { float Rs, Rp, Ts, Tp; };

Fresnel fresnel(vec3 incident, vec3 normal, float n1, float n2)
{
    float dotNI = dot(incident, normal);
    float eta = n1 / n2;
    float c1 = -dotNI;
    float c2 = 1.0 - (1.0 - c1 * c1) * (eta * eta);
    Fresnel f;
    if (c2 < 0.0)
205 {
        // total internal reflection
        f.Rs = 1.0;
        f.Rp = 1.0;
        f.Ts = 0.0;
210     f.Tp = 0.0;
    }
    else
    {
        c2 = sqrt(c2);
215     float rs = (eta * c1 - c2) / (eta * c1 + c2);
        float rp = (eta * c2 - c1) / (eta * c2 + c1);
        float ts = 2.0 * eta * c1 / (eta * c1 + c2);
        float tp = 2.0 * eta * c1 / (eta * c2 + c1);
        f.Rs = rs * rs;
220     f.Rp = rp * rp;
        f.Ts = ts * ts;
        f.Tp = tp * tp;
    }
    return f;
225 }

// refractive materials

float Transparent(Random PRNG, float S, Ray V, vec2 index)
230 {
    return S;
}

Hit Transparent(Random PRNG, Surface S, Ray V, vec2 index)
235 {
    V.origin = S.position;
    vec2 nk1 = V.index;
    vec2 nk2 = index;
    bool inside = false;
240     if (dot(-V.direction, S.normal) < 0.0)
    {
        nk1 = nk2;
        nk2 = vec2(1.0, 0.0); // vacuum
        S = Invert(S);
245     inside = true;
    }
}

```

```

    Fresnel F = fresnel(V.direction, S.normal, nk1.x, nk2.x);
    // FIXME polarization
    float R = 0.5 * (F.Rs + F.Rp);
250   float T = 0.5 * (F.Ts + F.Tp);
    float RT = R + T;
    float hRT = halton1(PRNG);
    if (mix(0.0, RT, hRT) <= R)
    {
255       V.direction = normalize(reflect(V.direction, S.normal));
        V.index = nk1;
    }
    else
    {
260       V.direction = normalize(refract(V.direction, S.normal, nk1.x / nk2.x));
        V.index = nk2;
    }
    if (inside)
    {
265       S = Invert(S);
    }
    Hit h;
    h.surface = S;
    h.ray = V;
270   h.factor = 1.0;
    h.emit = 0.0;
    return h;
}

275 // thin film soap bubble

float SoapBubble(Random PRNG, float S, Ray V, float thickness, vec2 index)
{
    return S;
280 }

Hit SoapBubble(Random PRNG, Surface S, Ray V, float thickness, vec2 index)
{
    V.origin = S.position;
285   vec2 nk_air = V.index;
    vec2 nk_film = index;
    bool inside = false;
    if (dot(-V.direction, S.normal) < 0.0)
    {
290       S = Invert(S);
        inside = true;
    }
    vec3 refracted = normalize(refract(V.direction, S.normal, nk_air.x / nk_film.x,
    ↵ ));
    Fresnel F_in = fresnel(V.direction, S.normal, nk_air.x, nk_film.x);
295   Fresnel F_out = fresnel(refracted, S.normal, nk_film.x, nk_air.x);
    // FIXME polarization, absorption
    float T_in = 0.5 * (F_in.Ts + F_in.Tp);
    float T_out = 0.5 * (F_out.Ts + F_out.Tp);
    float R_in = 0.5 * (F_in.Rs + F_in.Rp);
300   float R_film = 0.5 * (F_out.Rs + F_out.Rp);
    float d = 2.0 * pi * thickness / V.wavelength / abs(dot(refracted, S.normal));
    vec2 D = vec2(cos(d), sin(d));

```

```

    vec2 D2 = cSqr(D);
    vec2 one = vec2(1.0, 0.0);
305    float T = length(cDiv(T_in * T_out * D, one - R_film * R_film * D2));
    float R = length(cDiv(T_in * T_out * R_film * D2, one - R_film * R_film * D2)) ↵
        ↵ - vec2(R_in, 0.0));
    float hRT = halton1(PRNG) * (R + T);
    if (hRT < R)
    {
310        V.direction = normalize(reflect(V.direction, S.normal));
    }
    // otherwise ray continues in same direction
    if (inside)
    {
315        S = Invert(S);
    }
    Hit h;
    h.surface = S;
    h.ray = V;
320    h.factor = 1.0;
    h.emit = 0.0;
    return h;
}

325 // reflective thin film

float ThinFilm(float S, Ray V, float thickness, float factor)
{
    return S;
330 }

Hit ThinFilm(Surface S, Ray V, float thickness, float factor)
{
    float t = 4.0 * pi * (-dot(V.direction, S.normal)) * thickness / V.wavelength;
335    float f = 0.5 * length(vec2(cos(t) + 1.0, sin(t)));
    V.direction = reflect(V.direction, S.normal);
    Hit h;
    h.surface = S;
    h.ray = V;
340    h.factor = factor * f;
    h.emit = 0.0;
    return h;
}

345 float Checkerboard(vec3 x, float a, float b)
{
    x -= floor(x);
    bool c = (x.x > 0.5) != (x.y > 0.5) != (x.z > 0.5);
    return c ? a : b;
350 }

Hit Checkerboard(vec3 x, Hit a, Hit b)
{
    x -= floor(x);
355    bool c = (x.x > 0.5) != (x.y > 0.5) != (x.z > 0.5);
    return c ? a : b;
}

```

```

float absorption(float k, float nm, float dist)
360 {
    return exp(-4.0 * pi * k * dist / (1.0e-9 * nm));
}

```

25 include/Raymond-Observer.frag

```
#donotrun
```

```

/*
Raymond - a physics-inspired ray tracer for Fragmentarium
5 Copyright (C) 2018 Claude Heiland-Allen
License GPL3+ <http://www.gnu.org/licenses/>
*/

// linear XYZ to linear RGB
10 // https://en.wikipedia.org/wiki/SRGB#The_forward_transformation_(↗
    ↘ CIE_XYZ_to_sRGB)
vec3 xyz2rgb(in vec3 l)
{
    const vec3 whitePoint = vec3(0.9505, 1.0000, 1.0890);
    const mat3 matrix = mat3
15     ( 3.2406, -1.5372, -0.4986
        , -0.9689, 1.8758, 0.0415
        , 0.0557, -0.2040, 1.0570
        );
    return (whitePoint * l) * matrix;
20 }

// linear RGB to linear XYZ
// https://en.wikipedia.org/wiki/SRGB#The_reverse_transformation
vec3 rgb2xyz(in vec3 l)
25 {
    const vec3 whitePoint = vec3(0.9505, 1.0000, 1.0890);
    const mat3 matrix = mat3
        ( 0.4124, 0.3576, 0.1805
          , 0.2126, 0.7152, 0.0722
30      , 0.0193, 0.1192, 0.9505
        );
    return (l * matrix) / whitePoint;
}

35 // CIE standard observer
// https://en.wikipedia.org/wiki/CIE_1931_color_space#CIE_standard_observer
vec3 observer(in float wavelength)
{
    const int wavelength_min = 390;
40 const int wavelength_max = 830;
#define wavelength_count 441
const vec3 tristimulus_curve[wavelength_count] = vec3[wavelength_count]
    ( vec3(3.769647e-3, 4.146161e-4, 1.847260e-2)
      , vec3(4.532416e-3, 5.028333e-4, 2.221101e-2)
45      , vec3(5.446553e-3, 6.084991e-4, 2.669819e-2)
      , vec3(6.538868e-3, 7.344436e-4, 3.206937e-2)
      , vec3(7.839699e-3, 8.837389e-4, 3.847832e-2)
      , vec3(9.382967e-3, 1.059646e-3, 4.609784e-2)
      , vec3(1.120608e-2, 1.265532e-3, 5.511953e-2)
    )

```



```

50      , vec3(1.334965e-2, 1.504753e-3, 6.575257e-2)
      , vec3(1.585690e-2, 1.780493e-3, 7.822113e-2)
      , vec3(1.877286e-2, 2.095572e-3, 9.276013e-2)
      , vec3(2.214302e-2, 2.452194e-3, 1.096090e-1)
      , vec3(2.601285e-2, 2.852216e-3, 1.290077e-1)
55      , vec3(3.043036e-2, 3.299115e-3, 1.512047e-1)
      , vec3(3.544325e-2, 3.797466e-3, 1.764441e-1)
      , vec3(4.109640e-2, 4.352768e-3, 2.049517e-1)
      , vec3(4.742986e-2, 4.971717e-3, 2.369246e-1)
      , vec3(5.447394e-2, 5.661014e-3, 2.725123e-1)
60      , vec3(6.223612e-2, 6.421615e-3, 3.117820e-1)
      , vec3(7.070048e-2, 7.250312e-3, 3.547064e-1)
      , vec3(7.982513e-2, 8.140173e-3, 4.011473e-1)
      , vec3(8.953803e-2, 9.079860e-3, 4.508369e-1)
      , vec3(9.974848e-2, 1.005608e-2, 5.034164e-1)
65      , vec3(1.104019e-1, 1.106456e-2, 5.586361e-1)
      , vec3(1.214566e-1, 1.210522e-2, 6.162734e-1)
      , vec3(1.328741e-1, 1.318014e-2, 6.760982e-1)
      , vec3(1.446214e-1, 1.429377e-2, 7.378822e-1)
      , vec3(1.566468e-1, 1.545004e-2, 8.013019e-1)
70      , vec3(1.687901e-1, 1.664093e-2, 8.655573e-1)
      , vec3(1.808328e-1, 1.785302e-2, 9.295791e-1)
      , vec3(1.925216e-1, 1.907018e-2, 9.921293e-1)
      , vec3(2.035729e-1, 2.027369e-2, 1.051821)
      , vec3(2.137531e-1, 2.144805e-2, 1.107509)
75      , vec3(2.231348e-1, 2.260041e-2, 1.159527)
      , vec3(2.319245e-1, 2.374789e-2, 1.208869)
      , vec3(2.403892e-1, 2.491247e-2, 1.256834)
      , vec3(2.488523e-1, 2.612106e-2, 1.305008)
      , vec3(2.575896e-1, 2.739923e-2, 1.354758)
80      , vec3(2.664991e-1, 2.874993e-2, 1.405594)
      , vec3(2.753532e-1, 3.016909e-2, 1.456414)
      , vec3(2.838921e-1, 3.165145e-2, 1.505960)
      , vec3(2.918246e-1, 3.319038e-2, 1.552826)
      , vec3(2.989200e-1, 3.477912e-2, 1.595902)
85      , vec3(3.052993e-1, 3.641495e-2, 1.635768)
      , vec3(3.112031e-1, 3.809569e-2, 1.673573)
      , vec3(3.169047e-1, 3.981843e-2, 1.710604)
      , vec3(3.227087e-1, 4.157940e-2, 1.748280)
      , vec3(3.288194e-1, 4.337098e-2, 1.787504)
90      , vec3(3.349242e-1, 4.517180e-2, 1.826609)
      , vec3(3.405452e-1, 4.695420e-2, 1.863108)
      , vec3(3.451688e-1, 4.868718e-2, 1.894332)
      , vec3(3.482554e-1, 5.033657e-2, 1.917479)
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365      , vec3(4.477579e-3, 1.713976e-3, 0.000000)
      , vec3(4.150166e-3, 1.588899e-3, 0.000000)
      , vec3(3.847988e-3, 1.473453e-3, 0.000000)
      , vec3(3.569452e-3, 1.367022e-3, 0.000000)
      , vec3(3.312857e-3, 1.268954e-3, 0.000000)
370      , vec3(3.076022e-3, 1.178421e-3, 0.000000)
      , vec3(2.856894e-3, 1.094644e-3, 0.000000)
      , vec3(2.653681e-3, 1.016943e-3, 0.000000)
      , vec3(2.464821e-3, 9.447269e-4, 0.000000)
      , vec3(2.289060e-3, 8.775171e-4, 0.000000)
375      , vec3(2.125694e-3, 8.150438e-4, 0.000000)
      , vec3(1.974121e-3, 7.570755e-4, 0.000000)
      , vec3(1.833723e-3, 7.033755e-4, 0.000000)
      , vec3(1.703876e-3, 6.537050e-4, 0.000000)
      , vec3(1.583904e-3, 6.078048e-4, 0.000000)
380      , vec3(1.472939e-3, 5.653435e-4, 0.000000)
      , vec3(1.370151e-3, 5.260046e-4, 0.000000)
      , vec3(1.274803e-3, 4.895061e-4, 0.000000)
      , vec3(1.186238e-3, 4.555970e-4, 0.000000)
      , vec3(1.103871e-3, 4.240548e-4, 0.000000)
385      , vec3(1.027194e-3, 3.946860e-4, 0.000000)
      , vec3(9.557493e-4, 3.673178e-4, 0.000000)
      , vec3(8.891262e-4, 3.417941e-4, 0.000000)
      , vec3(8.269535e-4, 3.179738e-4, 0.000000)
      , vec3(7.689351e-4, 2.957441e-4, 0.000000)
390      , vec3(7.149425e-4, 2.750558e-4, 0.000000)
      , vec3(6.648590e-4, 2.558640e-4, 0.000000)

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, vec3(6.185421e-4, 2.381142e-4, 0.000000)
, vec3(5.758303e-4, 2.217445e-4, 0.000000)
, vec3(5.365046e-4, 2.066711e-4, 0.000000)
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, vec3(4.665005e-4, 1.798315e-4, 0.000000)
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, vec3(3.287199e-4, 1.269451e-4, 0.000000)
, vec3(3.063998e-4, 1.183671e-4, 0.000000)
, vec3(2.856577e-4, 1.103928e-4, 0.000000)
, vec3(2.664108e-4, 1.029908e-4, 0.000000)
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, vec3(2.319529e-4, 8.973323e-5, 0.000000)
, vec3(2.165300e-4, 8.379694e-5, 0.000000)
, vec3(2.021853e-4, 7.827442e-5, 0.000000)
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, vec3(1.647895e-4, 6.387035e-5, 0.000000)
, vec3(1.539542e-4, 5.969389e-5, 0.000000)
, vec3(1.438270e-4, 5.578862e-5, 0.000000)
, vec3(1.343572e-4, 5.213509e-5, 0.000000)
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, vec3(1.172706e-4, 4.553845e-5, 0.000000)
, vec3(1.095983e-4, 4.257443e-5, 0.000000)
, vec3(1.024685e-4, 3.981884e-5, 0.000000)
, vec3(9.584715e-5, 3.725877e-5, 0.000000)
420 , vec3(8.968316e-5, 3.487467e-5, 0.000000)
, vec3(8.392734e-5, 3.264765e-5, 0.000000)
, vec3(7.853708e-5, 3.056140e-5, 0.000000)
, vec3(7.347551e-5, 2.860175e-5, 0.000000)
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, vec3(6.008292e-5, 2.341373e-5, 0.000000)
, vec3(5.620098e-5, 2.190914e-5, 0.000000)
, vec3(5.259870e-5, 2.051259e-5, 0.000000)
, vec3(4.926279e-5, 1.921902e-5, 0.000000)
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, vec3(4.328212e-5, 1.689899e-5, 0.000000)
, vec3(4.058715e-5, 1.585309e-5, 0.000000)
, vec3(3.806114e-5, 1.487243e-5, 0.000000)
, vec3(3.568818e-5, 1.395085e-5, 0.000000)
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, vec3(3.137090e-5, 1.227327e-5, 0.000000)
, vec3(2.941371e-5, 1.151233e-5, 0.000000)
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, vec3(2.276639e-5, 8.925630e-6, 0.000000)
, vec3(2.136009e-5, 8.377852e-6, 0.000000)
, vec3(2.004122e-5, 7.863920e-6, 0.000000)
, vec3(1.880380e-5, 7.381539e-6, 0.000000)
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, vec3(1.655671e-5, 6.505136e-6, 0.000000)
, vec3(1.553939e-5, 6.108221e-6, 0.000000)
, vec3(1.458792e-5, 5.736935e-6, 0.000000)

```

```

    , vec3(1.369853e-5, 5.389831e-6, 0.000000)
450  , vec3(1.286705e-5, 5.065269e-6, 0.000000)
    , vec3(1.208947e-5, 4.761667e-6, 0.000000)
    , vec3(1.136207e-5, 4.477561e-6, 0.000000)
    , vec3(1.068141e-5, 4.211597e-6, 0.000000)
    , vec3(1.004411e-5, 3.962457e-6, 0.000000)
455  , vec3(9.446399e-6, 3.728674e-6, 0.000000)
    , vec3(8.884754e-6, 3.508881e-6, 0.000000)
    , vec3(8.356050e-6, 3.301868e-6, 0.000000)
    , vec3(7.857521e-6, 3.106561e-6, 0.000000)
    , vec3(7.386996e-6, 2.922119e-6, 0.000000)
460  , vec3(6.943576e-6, 2.748208e-6, 0.000000)
    , vec3(6.526548e-6, 2.584560e-6, 0.000000)
    , vec3(6.135087e-6, 2.430867e-6, 0.000000)
    , vec3(5.768284e-6, 2.286786e-6, 0.000000)
    , vec3(5.425069e-6, 2.151905e-6, 0.000000)
465  , vec3(5.103974e-6, 2.025656e-6, 0.000000)
    , vec3(4.803525e-6, 1.907464e-6, 0.000000)
    , vec3(4.522350e-6, 1.796794e-6, 0.000000)
    , vec3(4.259166e-6, 1.693147e-6, 0.000000)
    , vec3(4.012715e-6, 1.596032e-6, 0.000000)
470  , vec3(3.781597e-6, 1.504903e-6, 0.000000)
    , vec3(3.564496e-6, 1.419245e-6, 0.000000)
    , vec3(3.360236e-6, 1.338600e-6, 0.000000)
    , vec3(3.167765e-6, 1.262556e-6, 0.000000)
    , vec3(2.986206e-6, 1.190771e-6, 0.000000)
475  , vec3(2.814999e-6, 1.123031e-6, 0.000000)
    , vec3(2.653663e-6, 1.059151e-6, 0.000000)
    , vec3(2.501725e-6, 9.989507e-7, 0.000000)
    , vec3(2.358723e-6, 9.422514e-7, 0.000000)
    , vec3(2.224206e-6, 8.888804e-7, 0.000000)
480  , vec3(2.097737e-6, 8.386690e-7, 0.000000)
    , vec3(1.978894e-6, 7.914539e-7, 0.000000)
    , vec3(1.867268e-6, 7.470770e-7, 0.000000)
    , vec3(1.762465e-6, 7.053860e-7, 0.000000)
);
485 float l = wavelength - wavelength_min;
    int i0 = int(floor(l));
    int i1 = i0 + 1;
    float f1 = l - float(i0);
    if (i0 < 0) return vec3(0.0);
490  if (i1 > wavelength_count - 1) return vec3(0.0);
    return mix(tristimulus_curve[i0], tristimulus_curve[i1], f1);
#undef wavelength_count
}

```

26 include/Raymond-Pinhole.frag

```
#donotrun
```

```

/*
Raymond - a physics-inspired ray tracer for Fragmentarium
5  Copyright (C) 2018 Claude Heiland-Allen
    License GPL3+ <http://www.gnu.org/licenses/>
*/

```

```
#group Pinhole
```



```

10 // Pinhole aperture radius and depth (mm)
uniform vec2 Aperture; slider[(0,0),(0.1,0.01),(10.0,10.0)]

// Size of film plane of camera (mm)
15 uniform float Size; slider[0.0,35.0,1000.0]

// Range of light wavelengths to trace (nm)
uniform vec2 Wavelengths; slider[(0.0,0.0),(300.0,780.0),(1000.0,1000.0)]

20 struct Pinhole
{
    vec2 aperture; // m
    float size; // m
    vec2 wavelengths; // nm
25 };

Pinhole pinhole_uniforms()
{
    Pinhole P;
30 P.aperture = Aperture / 1000.0;
P.size = Size / 1000.0;
P.wavelengths = Wavelengths;
return P;
}

35 Ray pinhole(Random PRNG, Camera C, vec2 pixel, Pinhole P, out float intensity)
{
    vec2 rect = halton2(srand(PRNG, 1));
    vec2 disc = haltonDisc(srand(PRNG, 2));
40 float wave = halton1(srand(PRNG, 3));
float dist = P.size / 2.0 / tan(C.fieldOfView / 2.0);
vec2 p = pixel + dFdx(pixel) * rect.x + dFdy(pixel) * rect.y;
vec3 from = C.origin - dist * C.Z + P.size / 2.0 * (p.x * C.X + p.y * C.Y);
vec3 to = C.origin + P.aperture.x * (disc.x * C.X + disc.y * C.Y);
45 Ray V;
V.origin = to;
V.direction = normalize(to - from);
V.wavelength = mix(P.wavelengths.x, P.wavelengths.y, wave);
V.index = vec2(1.0, 0.0); // vacuum
50 // vignette
// <http://www.galerie-photo.com/stenope-cercle-image-theorie.html>
float a = acos(clamp(dot(C.Z, V.direction), 0.0, 1.0));
float t = tan(a);
float d = P.aperture.x * 2.0;
55 float e = P.aperture.y;
float ted = clamp(t * e / d, 0.0, 1.0);
intensity = acos(ted) - t * e * d * sqrt(1.0 - ted * ted);
return V;
}

```

27 include/Raymond-Quartz.frag

```
#donotrun
```

```
/*
Raymond - a physics-inspired ray tracer for Fragmentarium

```

```
5  Copyright (C) 2018  Claude Heiland-Allen
   License GPL3+ <http://www.gnu.org/licenses/>
   */

vec2 Quartz_nk(float wavelength) {
10   const float quartz_min  = 390;
   const float quartz_step  = 2;
   #define quartz_count 221
   const vec2 quartz_nk[quartz_count] = vec2[quartz_count]
15     ( vec2(1.490867, 0.000009)
     , vec2(1.490629, 0.000007)
     , vec2(1.490396, 0.000005)
     , vec2(1.490165, 0.000003)
     , vec2(1.489938, 0.000002)
     , vec2(1.489714, 0.000001)
20     , vec2(1.489494, 0.000001)
     , vec2(1.489276, 0.000000)
     , vec2(1.489062, 0.000000)
     , vec2(1.488850, 0.000000)
     , vec2(1.488641, 0.000000)
25     , vec2(1.488435, 0.000000)
     , vec2(1.488231, 0.000000)
     , vec2(1.488031, 0.000000)
     , vec2(1.487833, 0.000000)
     , vec2(1.487638, 0.000000)
30     , vec2(1.487446, 0.000000)
     , vec2(1.487256, 0.000000)
     , vec2(1.487069, 0.000000)
     , vec2(1.486884, 0.000000)
     , vec2(1.486702, 0.000000)
35     , vec2(1.486522, 0.000000)
     , vec2(1.486345, 0.000000)
     , vec2(1.486170, 0.000000)
     , vec2(1.485997, 0.000000)
     , vec2(1.485827, 0.000000)
40     , vec2(1.485659, 0.000000)
     , vec2(1.485493, 0.000000)
     , vec2(1.485329, 0.000000)
     , vec2(1.485167, 0.000000)
     , vec2(1.485008, 0.000000)
45     , vec2(1.484851, 0.000000)
     , vec2(1.484695, 0.000000)
     , vec2(1.484542, 0.000000)
     , vec2(1.484390, 0.000000)
     , vec2(1.484241, 0.000000)
50     , vec2(1.484094, 0.000000)
     , vec2(1.483948, 0.000000)
     , vec2(1.483804, 0.000000)
     , vec2(1.483662, 0.000000)
     , vec2(1.483522, 0.000000)
55     , vec2(1.483383, 0.000000)
     , vec2(1.483247, 0.000000)
     , vec2(1.483111, 0.000000)
     , vec2(1.482978, 0.000000)
     , vec2(1.482846, 0.000000)
60     , vec2(1.482716, 0.000000)
     , vec2(1.482588, 0.000000)
```

```
        , vec2(1.482461, 0.000000)
        , vec2(1.482335, 0.000000)
        , vec2(1.482211, 0.000000)
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        , vec2(1.481968, 0.000000)
        , vec2(1.481848, 0.000000)
        , vec2(1.481730, 0.000000)
        , vec2(1.481613, 0.000000)
70      , vec2(1.481498, 0.000000)
        , vec2(1.481384, 0.000000)
        , vec2(1.481271, 0.000000)
        , vec2(1.481160, 0.000000)
        , vec2(1.481050, 0.000000)
75      , vec2(1.480941, 0.000000)
        , vec2(1.480834, 0.000000)
        , vec2(1.480727, 0.000000)
        , vec2(1.480622, 0.000000)
        , vec2(1.480518, 0.000000)
80      , vec2(1.480416, 0.000000)
        , vec2(1.480314, 0.000000)
        , vec2(1.480214, 0.000000)
        , vec2(1.480115, 0.000000)
        , vec2(1.480016, 0.000000)
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        , vec2(1.479823, 0.000000)
        , vec2(1.479729, 0.000000)
        , vec2(1.479635, 0.000000)
        , vec2(1.479542, 0.000000)
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        , vec2(1.479269, 0.000000)
        , vec2(1.479181, 0.000000)
        , vec2(1.479093, 0.000000)
95      , vec2(1.479006, 0.000000)
        , vec2(1.478920, 0.000000)
        , vec2(1.478835, 0.000000)
        , vec2(1.478751, 0.000000)
        , vec2(1.478667, 0.000000)
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        , vec2(1.478503, 0.000000)
        , vec2(1.478423, 0.000000)
        , vec2(1.478343, 0.000000)
        , vec2(1.478264, 0.000000)
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        , vec2(1.478108, 0.000000)
        , vec2(1.478032, 0.000000)
        , vec2(1.477956, 0.000000)
        , vec2(1.477881, 0.000000)
110     , vec2(1.477807, 0.000000)
        , vec2(1.477733, 0.000000)
        , vec2(1.477660, 0.000000)
        , vec2(1.477588, 0.000000)
        , vec2(1.477517, 0.000000)
115     , vec2(1.477447, 0.000000)
        , vec2(1.477377, 0.000000)
        , vec2(1.477308, 0.000000)
        , vec2(1.477239, 0.000000)
```

```
120      , vec2(1.477171, 0.000000)
      , vec2(1.477104, 0.000000)
      , vec2(1.477038, 0.000000)
      , vec2(1.476972, 0.000000)
      , vec2(1.476907, 0.000000)
      , vec2(1.476842, 0.000000)
125      , vec2(1.476778, 0.000000)
      , vec2(1.476715, 0.000000)
      , vec2(1.476652, 0.000000)
      , vec2(1.476590, 0.000000)
      , vec2(1.476529, 0.000000)
130      , vec2(1.476468, 0.000000)
      , vec2(1.476408, 0.000000)
      , vec2(1.476348, 0.000000)
      , vec2(1.476289, 0.000000)
      , vec2(1.476230, 0.000000)
135      , vec2(1.476172, 0.000000)
      , vec2(1.476115, 0.000000)
      , vec2(1.476058, 0.000000)
      , vec2(1.476001, 0.000000)
      , vec2(1.475946, 0.000000)
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      , vec2(1.475781, 0.000000)
      , vec2(1.475727, 0.000000)
      , vec2(1.475674, 0.000000)
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      , vec2(1.475517, 0.000000)
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      , vec2(1.475022, 0.000000)
      , vec2(1.474975, 0.000000)
      , vec2(1.474929, 0.000000)
160      , vec2(1.474883, 0.000000)
      , vec2(1.474837, 0.000000)
      , vec2(1.474791, 0.000000)
      , vec2(1.474746, 0.000000)
      , vec2(1.474702, 0.000000)
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      , vec2(1.474570, 0.000000)
      , vec2(1.474527, 0.000000)
      , vec2(1.474484, 0.000000)
170      , vec2(1.474442, 0.000000)
      , vec2(1.474400, 0.000000)
      , vec2(1.474358, 0.000000)
      , vec2(1.474317, 0.000000)
      , vec2(1.474276, 0.000000)
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```

```
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, vec2(1.473922, 0.000000)
, vec2(1.473884, 0.000000)
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, vec2(1.473810, 0.000000)
, vec2(1.473773, 0.000000)
, vec2(1.473737, 0.000000)
, vec2(1.473700, 0.000000)
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, vec2(1.473629, 0.000000)
, vec2(1.473594, 0.000000)
, vec2(1.473559, 0.000000)
, vec2(1.473524, 0.000000)
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, vec2(1.473387, 0.000000)
, vec2(1.473354, 0.000000)
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, vec2(1.473255, 0.000000)
, vec2(1.473223, 0.000000)
, vec2(1.473191, 0.000000)
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, vec2(1.473096, 0.000000)
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, vec2(1.473034, 0.000000)
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, vec2(1.472883, 0.000000)
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, vec2(1.472795, 0.000000)
, vec2(1.472766, 0.000000)
, vec2(1.472737, 0.000000)
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, vec2(1.472680, 0.000000)
, vec2(1.472652, 0.000000)
, vec2(1.472625, 0.000000)
, vec2(1.472597, 0.000000)
225 , vec2(1.472570, 0.000000)
, vec2(1.472542, 0.000000)
, vec2(1.472515, 0.000000)
, vec2(1.472489, 0.000000)
, vec2(1.472462, 0.000000)
230 , vec2(1.472436, 0.000000)
, vec2(1.472409, 0.000000)
, vec2(1.472383, 0.000000)
```

```

        , vec2(1.472357, 0.000000)
        , vec2(1.472332, 0.000000)
235    );
    float x = (wavelength - quartz_min) / quartz_step;
    int i0 = int(floor(x));
    int i1 = i0 + 1;
    float f1 = x - float(i0);
240    if (i0 < 0) return quartz_nk[0];
    if (i1 > quartz_count - 1) return quartz_nk[quartz_count - 1];
    vec2 y0 = quartz_nk[i0];
    vec2 y1 = quartz_nk[i1];
    return mix(y0, y1, f1);
245 #undef quartz_count
}

float Quartz(Random PRNG, float S, Ray V)
{
250    return S;
}

Hit Quartz(Random PRNG, Surface S, Ray V)
{
255    return Transparent(PRNG, S, V, Quartz_nk(V.wavelength));
}

```

28 include/Raymond-Quaternion.frag

```
#donotrun
```

```

/*
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*/

```

```

vec4 slerp(vec4 v0, vec4 v1, float t)
10 {
    float d = dot(v0, v1);
    if (d < 0.0)
    {
        v1 = -v1;
        d = -d;
15    }
    if (d > 0.9995)
    {
        return normalize(mix(v0, v1, t));
20    }
    float theta_0 = acos(d);
    float theta = theta_0 * t;
    float sin_theta = sin(theta);
    float sin_theta_0 = sin(theta_0);
25    float s0 = cos(theta) - d * sin_theta / sin_theta_0;
    float s1 = sin_theta / sin_theta_0;
    return s0 * v0 + s1 * v1;
}

30 vec3 qMul(vec4 q, vec3 v)

```

```

{
    vec3 t = 2.0 * cross(q.xyz, v);
    return v + q.w * t + cross(q.xyz, t);
}

```

35

```

vec4 qInv(vec4 q)
{
    return vec4(-q.xyz, q.w) / dot(q, q);
}

```

29 include/Raymond-Random.frag

```
#donotrun
```

```

/*
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*/

```

```
// uniforms in [0,1)^n
```

10

```

float uniform01(Random PRNG)
{
    return uniform01(PRNG.seed);
}

```

15

```

float uniform01(Random PRNG, int i)
{
    return uniform01(srand(PRNG, i));
}

```

20

```

float uniform1(Random PRNG)
{
    return uniform01(PRNG, 1);
}

```

25

```

vec2 uniform2(Random PRNG)
{
    return vec2(uniform01(PRNG, 1), uniform01(PRNG, 2));
}

```

30

```

vec3 uniform3(Random PRNG)
{
    return vec3(uniform01(PRNG, 1), uniform01(PRNG, 2), uniform01(PRNG, 3));
}

```

35

```

vec4 uniform4(Random PRNG)
{
    return vec4(uniform01(PRNG, 1), uniform01(PRNG, 2), uniform01(PRNG, 3),
        ↵ uniform01(PRNG, 4));
}

```

40

```
// uniform disc
```

```

vec2 uniformDiscNaive(vec2 u01)
{

```

```

45     float r = sqrt(u01.x);
        float t = 2.0 * pi * u01.y;
        return r * vec2(cos(t), sin(t));
    }

50 // http://www.pbr-book.org/3ed-2018/Monte-Carlo-Integration/2.2
    ↪ D_Sampling_with_Multidimensional_Transformations.html#SamplingaUnitDisk
    vec2 uniformDisc(vec2 u01)
    {
        vec2 u11 = 2.0 * u01 - vec2(1.0);
        if (u11 == vec2(0.0)) return u11;
55     float r, t;
        if (abs(u11.x) > abs(u11.y))
        {
            r = u11.x;
            t = pi / 4.0 * (u11.y / u11.x);
60     }
        else
        {
            r = u11.y;
            t = pi / 2.0 - pi / 4.0 * (u11.x / u11.y);
65     }
        return r * vec2(cos(t), sin(t));
    }

    vec2 uniformDisc(Random PRNG)
70 {
    return uniformDisc(uniform2(PRNG));
}

// Box-Muller transform
75
    vec2 gaussian(vec2 u01)
    {
        float s = u01.x;
        float t = 2.0 * pi * u01.y;
80     if (s > 0.0)
        return vec2(cos(t), sin(t)) * sqrt(-2.0 * log(s) / s);
        else
        return vec2(0.0);
    }

85
    vec2 gaussian2(Random PRNG)
    {
        return gaussian(uniform2(PRNG));
    }

90
    float gaussian1(Random PRNG)
    {
        return gaussian2(PRNG).x;
    }

95
    vec4 gaussian4(Random PRNG)
    {
        vec4 u = uniform4(PRNG);
        return vec4(gaussian(u.xy), gaussian(u.zw));
100 }

```



```

vec3 gaussian3(Random PRNG)
{
    return gaussian4(PRNG).xyz;
105 }

// a rotation matrix that makes Z point along the normal

mat3 localCoordinates(vec3 normal)
110 {
    vec3 w = X;
    if (abs(dot(Y, normal)) < abs(dot(w, normal))) w = Y;
    if (abs(dot(Z, normal)) < abs(dot(w, normal))) w = Z;
    vec3 a = normalize(cross(w, normal));
115 vec3 b = normalize(cross(a, normal));
    if (dot(normal, cross(a, b)) < 0.0) { vec3 t = a; a = b; b = t; }
    return mat3(a, b, normal);
}

120 // cosine weighted hemisphere from uniform disc and normal

vec3 cosHemisphere(vec2 uDisc, vec3 normal)
{
    mat3 m = localCoordinates(normal);
125 vec3 w = vec3(uDisc, sqrt(max(0.0, 1.0 - dot(uDisc, uDisc))));
    return m * w;
}

```

30 include/Raymond-Screen.frag

```

#donotrun

/*
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*/

float Screen_hump(vec3 spec, float wavelength)
10 {
    float delta = (wavelength - spec[0]) / spec[1];
    return spec[2] / (1.0 + 4.0 * delta * delta);
}

15 // <http://www.marcelpatek.com/LCD.html> (Figure 2)
float CRT(vec3 linearRGB, float wavelength)
{
    const vec3 r[2] = vec3[2]
        ( vec3(710.0, 25.0, 0.5)
20         , vec3(625.0, 25.0, 1.0)
        );
    const vec3 g =
        vec3(540.0, 100.0, 0.5);
    const vec3 b =
25         vec3(450.0, 100.0, 0.5);
    float v = 0.0;
    v += linearRGB.r * Screen_hump(r[0], wavelength);
}

```

```

    v += linearRGB.r * Screen_hump(r[1], wavelength);
    v += linearRGB.g * Screen_hump(g    , wavelength);
30   v += linearRGB.b * Screen_hump(b    , wavelength);
    return v;
}

// <http://www.marcelpatek.com/LCD.html> (Figure 3)
35 float LCD(vec3 linearRGB, float wavelength)
{
    const vec3 r[2] = vec3[2]
        ( vec3(710.0, 25.0, 0.1 * 0.8)
        , vec3(610.0, 15.0, 1.0 * 0.8)
40     );
    const vec3 g[3] = vec3[3]
        ( vec3(585.0, 25.0, 0.2)
        , vec3(545.0, 15.0, 1.0)
        , vec3(490.0, 20.0, 0.3)
45     );
    const vec3 b[3] = vec3[3]
        ( vec3(550.0, 25.0, 0.1 * 0.5)
        , vec3(590.0, 40.0, 0.9 * 0.5)
        , vec3(450.0, 50.0, 1.0 * 0.5)
50     );
    float v = 0.0;
    v += linearRGB.r * Screen_hump(r[0], wavelength);
    v += linearRGB.r * Screen_hump(r[1], wavelength);
    v += linearRGB.g * Screen_hump(g[0], wavelength);
55   v += linearRGB.g * Screen_hump(g[1], wavelength);
    v += linearRGB.g * Screen_hump(g[2], wavelength);
    v += linearRGB.b * Screen_hump(b[0], wavelength);
    v += linearRGB.b * Screen_hump(b[1], wavelength);
    v += linearRGB.b * Screen_hump(b[2], wavelength);
60   return v;
}

```

31 include/Raymond-SkyBox.frag

```

#donotrun

/*
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*/

// implement this
10 float screen(vec4 tex, float wavelength);

#group SkyBox

// equirectangular (360x180 degrees) texture for background
15 uniform sampler2D Background;

// distance from origin at which the cube map is drawn
uniform float Distance; slider[0,100,1000]

20 // no struct SkyBox as samplers can only be uniforms or function arguments

```

```

vec4 textureEqui(sampler2D sampler, vec3 dir)
{
    dir = normalize(dir);
25   vec2 coord = vec2(atan(dir.y, -dir.x) / (2.0 * pi), acos(-dir.z) / pi);
    return texture(sampler, coord);
}

vec4 SkyBox_texture(Transform T, Ray V)
30 {
    return textureEqui(Background, backwardN(T, V.direction));
}

float SkyBox_intensity(Transform T, Ray V)
35 {
    return screen(SkyBox_texture(T, V), V.wavelength);
}

float SkyBox(Scene_DE tag, Transform T, Ray V)
40 {
    return Distance - length(backwardP(T, V.origin));
}

Hit SkyBox(Scene_HIT tag, Transform T, Ray V)
45 {
    Scene_DE DE;
    Surface S;
    S.position = V.origin;
    S.normal = -normalize(V.origin);
50   S.de = SkyBox(DE, T, V);
    Hit h;
    h.surface = S;
    h.ray = V;
    h.factor = 0.0;
55   h.emit = SkyBox_intensity(T, V);
    return h;
}

```

32 include/Raymond-sRGB-Buffer.frag

```

#donotrun

/*
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*/

#vertex
10   varying vec2 coord;

void main(void)
{
15   gl_Position = gl_Vertex;
    coord = ((gl_ProjectionMatrix * gl_Vertex).xy + vec2(1.0)) * 0.5;
}

```

```

#endvertex
20   varying vec2 coord;

    uniform sampler2D frontbuffer;

25  #group Post

    uniform float Exposure; slider[0.0,1.0,100.0]

    float sRGB(float c)
30  {
        c = clamp(c, 0.0, 1.0);
        const float a = 0.055;
        if (c <= 0.0031308)
            return 12.92 * c;
35     else
        return (1.0 + a) * pow(c, 1.0 / 2.4) - a;
    }

    vec3 sRGB(vec3 c)
40  {
        return vec3(sRGB(c.x), sRGB(c.y), sRGB(c.z));
    }

    void main(void)
45  {
        vec4 tex = texture2D(frontbuffer, coord);
        vec3 c = sRGB(Exposure * tex.xyz / tex.a);
        gl_FragColor = vec4(c, 1.0);
    }

```

33 include/Raymond-sRGB.frag

```

#donotrun

/*
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*/

// accumulate linear RGBW and output as sRGB with exposure control
10 #buffer RGBA32F
    #buffershader "Raymond-sRGB-Buffer.frag"
    #group Post
    uniform float Exposure; slider[0.0,1.0,100.0]

15 // https://en.wikipedia.org/wiki/sRGB#The_forward_transformation_(↗
    ↘ CIE_XYZ_to_sRGB)
    float linear2sRGB(float c)
    {
        c = clamp(c, 0.0, 1.0);
        const float a = 0.055;
20     if (c <= 0.0031308)
        return 12.92 * c;
    }

```

```

    else
        return (1.0 + a) * pow(c, 1.0 / 2.4) - a;
}
25  vec3 linear2sRGB(vec3 c)
    {
        return vec3(linear2sRGB(c.x), linear2sRGB(c.y), linear2sRGB(c.z));
    }
30  // https://en.wikipedia.org/wiki/SRGB#The_reverse_transformation
    float sRGB2linear(float c)
    {
        c = clamp(c, 0.0, 1.0);
35  const float a = 0.055;
        if (c <= 0.04045)
            return c / 12.92;
        else
            return pow((c + a) / (1.0 + a), 2.4);
40  }

    vec3 sRGB2linear(vec3 c)
    {
        return vec3(sRGB2linear(c.x), sRGB2linear(c.y), sRGB2linear(c.z));
45  }

```

34 include/Raymond-StdDev-Buffer.frag

```

#donotrun

/*
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*/

#vertex
10  varying vec2 coord;

    void main(void)
    {
15  gl_Position = gl_Vertex;
        coord = ((gl_ProjectionMatrix * gl_Vertex).xy + vec2(1.0)) * 0.5;
    }

#endvertex
20  varying vec2 coord;

    uniform sampler2D frontbuffer;

25  vec3 stddev(vec3 v)
    {
        float m = v[1] / v[0];
        float s = sqrt(v[0] * v[2] - v[1] * v[1]) / v[0];
        return vec3(s);
30  }

```

```
void main(void)
{
    vec4 tex = texture2D(frontbuffer, coord);
35    vec3 c = stddev(tex.xyz / tex.a);
    gl_FragColor = vec4(c, 1.0);
}
```

35 include/Raymond-StdDev.frag

```
#donotrun

/*
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*/

#buffer RGBA32F
10 #buffershader "Raymond-StdDev-Buffer.frag"

vec3 film_stddev(Random PRNG, float wavelength, float intensity)
{
15     return vec3(1.0, intensity, intensity * intensity);
}
```

36 include/Raymond-Surface.frag

```
#donotrun

/*
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*/

// CSG invert
10 float Invert(float de)
{
    return -de;
}

15 Surface Invert(Surface s)
{
    s.normal = - s.normal;
    s.de = - s.de;
20     return s;
}

// CSG union: minimum by de
25 float Union(float a, float b)
{
    if (a < b) return a; else return b;
}
```

```

30  Surface Union(Surface a, Surface b)
    {
        if (a.de < b.de) return a; else return b;
    }

35  #define Union3(a,b,c) Union(Union(a, b), c)
    #define Union4(a,b,c,d) Union(Union(Union(a, b), c), d)
    #define Union5(a,b,c,d,e) Union(Union(Union(Union(a, b), c), d), e)
    #define Union6(a,b,c,d,e,f) Union(Union(Union(Union(Union(a, b), c), d), e), f)

40  // CSG intersection: maximum by de

    float Intersection(float a, float b)
    {
        if (a > b) return a; else return b;
45  }

    Surface Intersection(Surface a, Surface b)
    {
        if (a.de > b.de) return a; else return b;
50  }

    #define Intersection3(a,b,c) Intersection(Intersection(a, b), c)
    #define Intersection4(a,b,c,d) Intersection(Intersection(Intersection(a, b), c),
        ↪ d)
    #define Intersection5(a,b,c,d,e) Intersection(Intersection(Intersection(↪
        ↪ Intersection(a, b), c), d), e)
55  #define Intersection6(a,b,c,d,e,f) Intersection(Intersection(Intersection(↪
        ↪ Intersection(Intersection(a, b), c), d), e), f)

    // primitives

    float Sphere(Scene_DE tag, Transform T, Ray V)
60  {
        return forwardD(T, length(backwardP(T, V.origin)) - 1.0);
    }

    Surface Sphere(Scene_HIT tag, Transform T, Ray V)
65  {
        vec3 world = V.origin;
        vec3 object = backwardP(T, world);
        vec3 normal = normalize(object);
        float de = length(object) - 1.0;
70  Surface s;
        s.position = forwardP(T, object);
        s.normal = forwardN(T, normal);
        s.de = forwardD(T, de);
        return s;
75  }

    float Plane(Scene_DE tag, Transform T, Ray V, vec3 normal, float dist)
    {
        return forwardD(T, dot(backwardP(T, V.origin), normalize(normal)) - dist);
80  }

    Surface Plane(Scene_HIT tag, Transform T, Ray V, vec3 normal, float dist)

```

```

{
    normal = normalize(normal);
85    vec3 world = V.origin;
    vec3 object = backwardP(T, world);
    float d = dot(object, normal) - dist;
    vec3 nearest = object - d * normal;
    Surface s;
90    s.position = forwardP(T, object);
    s.normal = forwardN(T, normal);
    nearest = forwardP(T, nearest);
    s.de = distance(s.position, nearest);
    if (d < 0.0)
95        s.de = - s.de;
    return s;
}

// https://iquilezles.org/www/articles/distfunctions/distfunctions.htm
100 float sdBox( vec3 p, vec3 b )
{
    vec3 d = abs(p) - b;
    return length(max(d,0.0))
        + min(max(d.x,max(d.y,d.z)),0.0); // remove this line for an only ↯
        ↪ partially signed sdf
105 }

float Cuboid(Scene_DE tag, Transform T, Ray V, vec3 size)
{
    return forwardD(T, sdBox(backwardP(T, V.origin), size));
110 }

Surface Cuboid(Scene_HIT tag, Transform T, Ray V, vec3 size)
{
    vec3 p = backwardP(T, V.origin);
115    float d = sdBox(p, size);
    float e = max(d, 1.0e-5 * length(size));
    vec3 n = vec3
        ( sdBox(p + e * X, size) - sdBox(p - e * X, size)
          , sdBox(p + e * Y, size) - sdBox(p - e * Y, size)
120          , sdBox(p + e * Z, size) - sdBox(p - e * Z, size)
        );
    Surface s;
    s.position = forwardP(T, p);
    s.normal = forwardN(T, normalize(n));
125    s.de = forwardD(T, d);
    return s;
}

float Cube(Scene_DE tag, Transform T, Ray V, float size)
130 {
    return Cuboid(tag, T, V, vec3(size));
}

Surface Cube(Scene_HIT tag, Transform T, Ray V, float size)
135 {
    return Cuboid(tag, T, V, vec3(size));
}

```



```

float Cube(Scene_DE tag, Transform T, Ray V)
140 {
    return Cube(tag, T, V, 1.0);
}

Surface Cube(Scene_HIT tag, Transform T, Ray V)
145 {
    return Cube(tag, T, V, 1.0);
}

```

37 include/Raymond-Trace.frag

```

#donotrun

/*
Raymond - a physics-inspired ray tracer for Fragmentarium
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*/

#group Raytrace
10 // Number of steps to march along each ray.
uniform int Steps; slider[0,100,1000]

// Maximum number of surface intersections per pixel.
15 uniform int Depth; slider[0,10,100]

// Stop tracing rays at this epsilon (in bits) to stop early.
uniform float MinDist; slider[-24.0,-16.0,8.0]

20 // Advance rays by this epsilon (in bits) to avoid repeated surface ↗
    ↘ intersections.
uniform float Acne; slider[-24.0,-12.0,8.0]

// Trace towards lights from each surface.
uniform bool SampleLights; checkbox[true]
25

struct Raytrace
{
    int steps;
    int depth;
30 float mindist;
    float acne;
    bool samplelights;
};

35 Raytrace raytrace_de_uniforms()
{
    Raytrace R;
    R.steps = Steps;
    R.depth = Depth;
40 R.mindist = pow(2.0, MinDist);
    R.acne = pow(2.0, Acne);
    R.samplelights = SampleLights;
    return R;
}

```

```

45 Hit raytrace_de_1(Random PRNG, Ray V, Raytrace R, float s)
{
    Scene_DE DE;
    int i = 0;
50 float d = scene(DE, srand(PRNG, i), V);
    for (; i < R.steps; ++i)
    {
        d = scene(DE, srand(PRNG, i), V);
        V.origin += s * d * V.direction;
55 // if (s * d < R.mindist) break;
    }
    Scene_HIT HIT;
    return scene(HIT, srand(PRNG, i), V);
}

60 float raytrace_de(Random PRNG, Ray V, Raytrace R, out Hit D)
{
    float I = 0.0;
    float f = 1.0;
65 float s = 1.0;
    for (int i = 0; i < R.depth; ++i)
    {
        // trace to surface
        Hit h = raytrace_de_1(srand(PRNG, i), V, R, s);
70 if (i == 0) D = h;
        f *= absorption(V.index.y, V.wavelength, distance(V.origin, h.ray.origin));
        if (R.samplelights)
        {
            // ignore lights from organic rays
75 if (h.emit > 0.0)
            {
                if (i == 0)
                {
                    I += f * h.emit;
80 f *= h.factor;
                }
                break;
            }
            f *= h.factor;
85 // trace from surface to lights
            Ray U = h.ray;
            vec4 L = light(srand(PRNG, i), U.origin, U.direction);
            if (L.w > 0.0)
            {
90 U.direction = normalize(L.xyz);
                U.origin += R.acne * U.direction;
                Hit l = raytrace_de_1(srand(PRNG, i), U, R, s);
                if (l.emit > 0.0)
                {
95 I += L.w * f * absorption(U.index.y, U.wavelength, distance(U.origin,
                    ↪ l.ray.origin)) * l.emit;
                }
            }
            f *= (1.0 - L.w);
        }
100 else

```

```

    {
        I += f * h.emit;
        f *= h.factor;
    }
105 // bounce
    V = h.ray;
    V.origin += R.acne * V.direction;
    Scene_HIT HIT;
    Surface S = scene(HIT, srand(PRNG, i + 1), V).surface;
110 float s2 = sign(S.de);
    float s3 = sign(dot(V.direction, S.normal));
    s = s2;
    if (! (f > 0)) break;
}
115 return I;
}

```

38 include/Raymond-Transform.frag

```

#donotrun

/*
Raymond - a physics-inspired ray tracer for Fragmentarium
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*/

// transformations
10
struct Transform
{
    mat4 forward; // object to world
    mat4 backward; // world to object
15 float scale; // forward
};

// composition of transformations

20 Transform compose(Transform S, Transform T)
{
    Transform R;
    R.forward = S.forward * T.forward;
    R.backward = T.backward * S.backward;
25 R.scale = S.scale * T.scale;
    return R;
}

Transform compose(Transform A, Transform B, Transform C)
30 {
    return compose(compose(A, B), C);
}

Transform compose(Transform A, Transform B, Transform C, Transform D)
35 {
    return compose(compose(compose(A, B), C), D);
}

```

```
// transformation of distances
40 float forwardD(Transform T, float d)
   {
       return d * T.scale;
   }
45 float backwardD(Transform T, float d)
   {
       return d / T.scale;
   }
50
// transformation of points
vec3 forwardP(Transform T, vec3 p)
55 {
    vec4 q = vec4(p, 1.0) * T.forward;
    return q.xyz / q.w;
}
60 vec3 backwardP(Transform T, vec3 p)
   {
       vec4 q = vec4(p, 1.0) * T.backward;
       return q.xyz / q.w;
   }
65
// transformation of normals
vec3 forwardN(Transform T, vec3 n)
   {
70     return normalize(n * inverse(transpose(mat3(T.forward))));
   }
vec3 backwardN(Transform T, vec3 n)
   {
75     return normalize(n * inverse(transpose(mat3(T.backward))));
   }
// uniform scaling
80 Transform Scale(float s)
   {
       Transform T;
       T.scale = s;
       T.forward = mat4
85         ( s, 0.0, 0.0, 0.0
           , 0.0, s, 0.0, 0.0
           , 0.0, 0.0, s, 0.0
           , 0.0, 0.0, 0.0, 1.0
         );
90     s = 1.0 / s;
       T.backward = mat4
           ( s, 0.0, 0.0, 0.0
           , 0.0, s, 0.0, 0.0
           , 0.0, 0.0, s, 0.0
95         , 0.0, 0.0, 0.0, 1.0
       );
   }
```

```

    );
    return T;
}

100 // identity transformation

Transform Identity()
{
    return Scale(1.0);
105 }

// non-uniform scaling

Transform Scale(vec3 s)
110 {
    Transform T;
    T.forward = mat4
        ( s.x, 0.0, 0.0, 0.0
          , 0.0, s.y, 0.0, 0.0
115   , 0.0, 0.0, s.z, 0.0
          , 0.0, 0.0, 0.0, 1.0
        );
    s = 1.0 / s;
    T.backward = mat4
120   ( s.x, 0.0, 0.0, 0.0
          , 0.0, s.y, 0.0, 0.0
          , 0.0, 0.0, s.z, 0.0
          , 0.0, 0.0, 0.0, 1.0
        );
125   T.scale = determinant(mat3(T.forward)); // FIXME
    return T;
}

// translation

130 Transform Translate(vec3 v)
{
    Transform T;
    T.scale = 1.0;
135   T.forward = (mat4
        ( 1.0, 0.0, 0.0, v.x
          , 0.0, 1.0, 0.0, v.y
          , 0.0, 0.0, 1.0, v.z
          , 0.0, 0.0, 0.0, 1.0
140   ));
    v = -v;
    T.backward = (mat4
        ( 1.0, 0.0, 0.0, v.x
          , 0.0, 1.0, 0.0, v.y
145   , 0.0, 0.0, 1.0, v.z
          , 0.0, 0.0, 0.0, 1.0
        ));
    return T;
}

150 // rotation from quaternion

```

```

Transform Rotate(vec4 q)
{
155   q = normalize(q);
      float i = q.x;
      float j = q.y;
      float k = q.z;
      float r = q.w;
160   Transform T;
      T.scale = 1.0;
      T.forward = mat4
        ( 1.0 - 2.0 * (j * j + k * k), 2.0 * (i * j - k * r), 2.0 * (i * k + j * r), ↵
          ↵ 0.0
          , 2.0 * (i * j + k * r), 1.0 - 2.0 * (i * i + k * k), 2.0 * (j * k - i * r), ↵
          ↵ 0.0
165   , 2.0 * (i * k - j * r), 2.0 * (j * k + i * r), 1.0 - 2.0 * (i * i + j * j), ↵
          ↵ 0.0
          , 0.0, 0.0, 0.0, 1.0
        );
      T.backward = transpose(T.forward);
      return T;
170 }

```

39 include/Raymond-Water.frag

```
#donotrun
```

```

/*
Raymond - a physics-inspired ray tracer for Fragmentarium
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   License GPL3+ <http://www.gnu.org/licenses/>
*/

```

```

vec2 Water_nk(float wavelength)
10 {
   const float water_min    = 375;
   const float water_step   = 25;
#define water_count 20
   const vec2  water_nk[water_count] = vec2[water_count]
15   ( vec2(1.341, 3.50E-9)
     , vec2(1.339, 1.86E-9)
     , vec2(1.338, 1.30E-9)
     , vec2(1.337, 1.02E-9)
     , vec2(1.336, 9.35E-10)
20   , vec2(1.335, 1.00E-9)
     , vec2(1.334, 1.32E-9)
     , vec2(1.333, 1.96E-9)
     , vec2(1.333, 3.60E-9)
     , vec2(1.332, 1.09E-8)
25   , vec2(1.332, 1.39E-8)
     , vec2(1.331, 1.64E-8)
     , vec2(1.331, 2.23E-8)
     , vec2(1.331, 3.35E-8)
     , vec2(1.330, 9.15E-8)
30   , vec2(1.330, 1.56E-7)
     , vec2(1.330, 1.48E-7)
     , vec2(1.329, 1.25E-7)
     , vec2(1.329, 1.82E-7)

```

```

    , vec2(1.329, 2.93E-7)
35  );
    float x = (wavelength - water_min) / water_step;
    int i0 = int(floor(x));
    int i1 = i0 + 1;
    float f1 = x - float(i0);
40  if (i0 < 0) return water_nk[0];
    if (i1 > water_count - 1) return water_nk[water_count - 1];
    vec2 y0 = water_nk[i0];
    vec2 y1 = water_nk[i1];
    return mix(y0, y1, f1);
45  #undef water_count
}

float Water(Random PRNG, float S, Ray V)
{
50  return S;
}

Hit Water(Random PRNG, Surface S, Ray V)
{
55  return Transparent(PRNG, S, V, Water_nk(V.wavelength));
}

```

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Version 3, 29 June 2007

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41 README.md

Raymond

A physics-inspired ray tracer for Fragmentarium.

5 ### Quick Start

Install git, install Fragmentarium.

Get the source code:

```
10     mkdir -p ~/opt/src
        cd ~/opt/src
        git clone https://code.mathr.co.uk/raymond.git
```

15 Configure Fragmentarium: menu Edit Preferences, set Include Path to

Examples/Include;/home/\$USER/opt/src/raymond/include

replacing ‘\$USER’ with your username.

20 Load ‘~/opt/src/raymond/examples/Balls.frag’ to see some shiny.

Legal

25 Raymond – a physics-inspired ray tracer for Fragmentarium

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