

snowglobe

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2012-2016

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## 1 back.png

mathr.co.uk

## 2 cards.sh

```
#!/bin/bash
pngtopnm < edge.png > edge.pgm
pngtopnm < back.png > back.pgm
mkdir 4x1
5 ls snowglobe-*.pgm | sort -R | xargs -n 4 pnmcats -lr | ( cd 4x1 ; pnmsplit )
```

```

mkdir 4x6
ls 4x1/* | xargs -n 6 pnmcat -tb | ( cd 4x6 ; pnmsplit )
mkdir 5x7
cd 4x6
10  for i in *
do
    pnmcat -tb -black ../edge.pgm $i ../edge.pgm |
    pgsplit white-black | pgsplit | pnmgamma 0.25 |
    pnmscale -ysize 1500 2100 | pnmcat -lr ../back.pgm - |
15  pnmtopng -force -interlace -phys 11811 11811 1 > ../5x7/$i.png
done
cd ../5x7
ls -lsh

```

### 3 edge.png



### 4 .gitignore

```

dist
.cabal-sandbox
cabal.sandbox.config

```

### 5 Hyperbolic.hs

```

module Hyperbolic where

import Data.Complex
import Vector

5  newtype H4 = H4{ unH4 :: V4 }
   newtype H2 = H2{ unH2 :: V2 }
   newtype H  = H{ unH  :: R  }

10  hdist :: H2 -> H2 -> H
     hdist (H2 z) (H2 w) = H $ acosh (1 + 2 * norm2 (z ^-^ w) / ((1 - norm2 z) * (1 -
       ↪ norm2 w)))

     h2e1 :: H -> R
     h2e1 (H z) = sqrt ((cosh z - 1) / (cosh z + 1))

15  h2e2 :: H2 -> V2
     h2e2 h@(H2 v) = norm v ^* h2e1 (hdist h (H2 o))
     e2h1 :: R -> H
     e2h1 z = hdist (H2 (V2 z 0)) (H2 o)

20  e2h2 :: V2 -> H2
     e2h2 z = H2 (norm z ^* (unH $ e2h1 (sqrt (norm2 z))))

     moebius :: H2 -> H4
25  moebius (H2 (V2 x y)) = H4 (V4 x y 1 0)

     unmoebius :: H4 -> H2

```

```

unmoebius (H4 (V4 a b c d)) = let (x:+y) = (a:+b)/(c:+d) in H2 (V2 x y)

30 mlength :: H4 -> R
   mlength (H4 (V4 a b c d)) = magnitude (a:+b) / magnitude (c:+d)

rotation :: R -> M4
rotation a = M4 c (-s) 0 0  s c 0 0  0 0 1 0  0 0 0 1
35   where
       c = cos a
       s = sin a

translation :: H2 -> M4
40 translation (H2 (V2 x y))
   | l > 0 = rotation (-s) ^^*^^ m ^^*^^ rotation s
   | otherwise = m
   where
       m = M4 f 0 g 0  0 f 0 g  g 0 f 0  0 g 0 f
45       s = phase (x:+y)
       l = magnitude (x:+y)
       e = exp l
       f = e + 1
       g = e - 1
50
rotationAbout :: H2 -> R -> M4
rotationAbout z@(H2 (V2 x y)) a = translation z ^^*^^ rotation a ^^*^^ ↯
    ↪ translation (H2 (V2 (-x) (-y)))

ecircle :: H2 -> H -> (V2, R)
55 ecircle c@(H2 (V2 cx cy)) (H hr) = (ec, er)
   where
       p = phase (cx :+ cy)
       a = unmoebius . H4 $ translation (H2 (V2 (-hr * cos p) (-hr * sin p))) ^^*^^ ↯
           ↪ unH4 (moebius c)
       b = unmoebius . H4 $ translation (H2 (V2 ( hr * cos p) ( hr * sin p))) ^^*^^ ↯
           ↪ unH4 (moebius c)
60       ea = h2e2 a
       eb = h2e2 b
       ec = (ea ^+^ eb) ^* 0.5
       er = 0.5 * (sqrt $ norm2 (ea ^-^ eb))

```

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```

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        MERCHANTABILITY or FITNESS FOR A PARTICULAR PURPOSE.  See the
645  GNU General Public License for more details.

        You should have received a copy of the GNU General Public License
        along with this program.  If not, see <http://www.gnu.org/licenses/>.

650  Also add information on how to contact you by electronic and paper mail.

        If the program does terminal interaction, make it output a short
        notice like this when it starts in an interactive mode:

655  <program> Copyright (C) <year> <name of author>
        This program comes with ABSOLUTELY NO WARRANTY; for details type 'show w'.
        This is free software, and you are welcome to redistribute it
        under certain conditions; type 'show c' for details.

660  The hypothetical commands 'show w' and 'show c' should show the appropriate
        parts of the General Public License.  Of course, your program's commands
        might be different; for a GUI interface, you would use an "about box".

        You should also get your employer (if you work as a programmer) or school,
665  if any, to sign a "copyright disclaimer" for the program, if necessary.
        For more information on this, and how to apply and follow the GNU GPL, see
        <http://www.gnu.org/licenses/>.

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670  into proprietary programs.  If your program is a subroutine library, you
        may consider it more useful to permit linking proprietary applications with
        the library.  If this is what you want to do, use the GNU Lesser General
        Public License instead of this License.  But first, please read
        <http://www.gnu.org/philosophy/why-not-lgpl.html>.

```

## 7 Setup.hs

```

import Distribution.Simple
main = defaultMain

```

## 8 snowglobe.cabal

```

Name:                snowglobe
Version:             3.0.0.3
Synopsis:             randomized fractal snowflakes demo
Description:          @snowglobe@ generates random snowflakes using iterated
5  function systems via OpenGL texture feedback.  The
                        snowflakes interact in a particle system.
                        .
Keyboard controls:
                        .
10  * f, F11: toggle full screen
                        .
                        * shift-R: toggle recording PPM images to stdout
                        .
                        * shift-S: toggle recording PGM images of each
15  generated flake to the current working directory
                        .
                        * any other key: quit

```



```

20         .
        Blog posts:
        .
        * <https://mathr.co.uk/blog/2012-01-12_snowglobe.html>
        .
        * <https://mathr.co.uk/blog/2014-12-19↵
          ↵ _making_seasonal_cards_with_snowglobe.html>

25 homepage:      https://code.mathr.co.uk/snowglobe
   License:      GPL-3
   License-file:  LICENSE
   Author:       Claude Heiland-Allen
   Maintainer:   claud@mathr.co.uk
30 Category:      Demo
   Build-type:   Simple
   Cabal-version: >=1.6

Executable snowglobe
35   Main-is:      SnowGlobe.hs
   other-modules: Vector
   GHC-options:   -Wall
   Build-depends:
40     base < 5,
       bytestring,
       containers,
       gl-capture,
       GLUT,
       OpenGL == 3.0.*,
45     OpenGLRaw,
       random

Source-repository head
   type:          git
50   location:     https://code.mathr.co.uk/snowglobe.git

Source-repository this
   type:          git
   location:     https://code.mathr.co.uk/snowglobe.git
55   tag:          v3.0.0.3

```

## 9 SnowGlobe.hs

```

-- SnowGlobe -- randomized fractal snowflakes demo
-- (GPL3+) 2012,2014,2015,2016 Claude Heiland-Allen <claud@mathr.co.uk>
-- tested with: ghc-7.6.3, ghc-7.8.2, ghc-7.10.1~rc2, ghc-8.0.1

```

```

5  import Vector hiding (i)
   import Graphics.UI.GLUT hiding (scale, FramebufferObject)
   import qualified Graphics.UI.GLUT as GL
   import Graphics.GL
     ( glTexImage2D
10    , glClampColor
     , glGenerateMipmap
     , glGenFramebuffers
     , glBindFramebuffer
     , glFramebufferTexture2D
15    , glUniformMatrix3fv

```

```

    , glGetTexImage
  )
import Graphics.GL.Tokens
{-
20   ( GL_TEXTURE_2D
    , GL_R32F
    , GL_RED
    , GL_RGBA
    , GL_UNSIGNED_BYTE
25   , GL_FALSE
    , GL_CLAMP_VERTEX_COLOR
    , GL_CLAMP_READ_COLOR
    , GL_CLAMP_FRAGMENT_COLOR
    , GL_ALPHA
30   , GL_FRAMEBUFFER
    , GL_COLOR_ATTACHMENT0
  )
-}
import Control.Exception (evaluate)
35 import Control.Monad (forM_, replicateM, when)
import Data.IORef (IORef, modifyIORef, newIORef, readIORef, writeIORef)
import Data.List (foldl', minimumBy)
import Data.Ord (comparing)
import Data.Map (Map)
40 import qualified Data.Map as M
import qualified Data.Set as S
import System.Exit (exitSuccess)
import System.IO (hPutStrLn, stderr, stdout, hPutStr, withBinaryFile, IOMode(
    ↪ WriteMode), hPutBuf)
import System.Random (randomRIO)
45 import Foreign (alloca, peek, nullPtr, withArray)
import Graphics.Rendering.OpenGL.Capture (capturePPM)
import Data.ByteString as BS (hPut, pack)
import Foreign (Ptr, allocaArray)
import Data.Word (Word8)
50
shader :: Maybe String -> Maybe String -> IO Program
shader mV mF = do
  p <- createProgram
  vs <- case mV of
55   Nothing -> return []
   Just v -> do
     vert <- createShader VertexShader
     shaderSourceBS vert $= BS.pack (map (toEnum . fromEnum) v)
     compileShader vert
60   msg <- get (shaderInfoLog vert)
     when (not (null msg)) $ hPutStrLn stderr msg
     return [vert]
  fs <- case mF of
65   Nothing -> return []
   Just f -> do
     frag <- createShader FragmentShader
     shaderSourceBS frag $= BS.pack (map (toEnum . fromEnum) f)
     compileShader frag
70   msg <- get (shaderInfoLog frag)
     when (not (null msg)) $ hPutStrLn stderr msg
     return [frag]

```

```

    attachedShaders p $= concat [vs, fs]
    linkProgram p
    msg <- get (programInfoLog p)
75    when (not (null msg)) $ hPutStrLn stderr msg
    return p

type N = Int

80    sum' :: Num a => [a] -> a
    sum' = foldl' (+) 0

    size :: N
    size = 2048

85    er :: R
    er = 4

    accuracy :: R
90    accuracy = 1 / fromIntegral size

    tSize :: N
    tSize = 1024

95    maxSpeed :: R
    maxSpeed = 10

data SnowGlobe = SnowGlobe
  { pInitial :: Program, pInitial'er, pInitial'rho :: UniformLocation
100    , pStep :: Program, pStep'er, pStep'ts, pStep'src :: UniformLocation
    , pColour :: Program, pColour'src, pColour'speed, pColour'colour :: UniformLocation
    , tPing, tPong :: TextureObject, fBuffer :: FramebufferObject
    , sFlakes :: [Flake], sTextures :: Map N TextureObject
    , wSize :: Size, wFullScreen :: Maybe Size
105    , sRenderFlake :: IO Render, sNextName :: N
    , sRecord, sRecordFlakes :: Bool
    }

data Flake = Flake
110    { flakeName :: !N
    , flakeTime :: !R
    , flakePosition :: !V2
    , flakeVelocity :: !V2
    }

115    flakeMass :: Flake -> R
    flakeMass f = let s = flakeSize f in 1 + s * s

    flakeSize :: Flake -> R
120    flakeSize f = sin (pi * flakeTime f)

    flakeForce :: Flake -> V2 -> V2
    flakeForce f p =
      let d@(V2 x y) = p ^^ flakePosition f
125      m = let d2 = x * x + y * y in d2 * d2
      in (flakeMass f / m) *^ d

```

```

flakeUpdate :: R -> [Flake] -> Flake -> Flake
flakeUpdate dt fs f = f
130   { flakeTime = flakeTime f + dt / 2
    , flakePosition = flakePosition f ^+^ (dt *^ flakeVelocity f)
    , flakeVelocity = mapVector ((* maxSpeed) . tanh . (/ maxSpeed)) $ 0.999 *^ (↵
      ↵ flakeVelocity f ^+^ ((dt / flakeMass f) *^ (flakeField fs (flakePosition ↵
      ↵ f))))
    }

135   mapVector :: (R -> R) -> V2 -> V2
mapVector f (V2 x y) = V2 (f x) (f y)

flakeField :: [Flake] -> V2 -> V2
flakeField fs p = foldl' (^+^) o [ flakeForce f (p ^+^ d) | f <- fs, p /= ↵
  ↵ flakePosition f, dx <- [-2,0,2], dy <- [-2,0,2], let d = V2 dx dy ]

140   flakeSpawn :: [Flake] -> N -> IO Flake
flakeSpawn fs name = do
  xs <- replicateM 32 $ randomRIO (-1, 1)
  ys <- replicateM 32 $ randomRIO (-1, 1)
145   let ps = zipWith V2 xs ys
      p = fst . minimumBy (comparing snd) . map (\p' -> (p', norm2 (flakeField ↵
      ↵ fs p')))) $ ps
  return Flake{ flakeName = name, flakeTime = 0, flakePosition = p, ↵
    ↵ flakeVelocity = o }
  where
    norm2 (V2 x y) = x * x + y * y

150   flakesUpdate :: R -> [Flake] -> [Flake]
flakesUpdate dt fs =
  let gs = map (flakeUpdate dt fs) fs
      alive = filter ((< 1) . flakeTime) gs
155   in map flakeWrap alive

flakeWrap :: Flake -> Flake
flakeWrap f = f{ flakePosition = mapVector wrap (flakePosition f) }
  where
160   wrap x =
    let y = (x + 1) / 2
        z = y - fromIntegral (floor y :: N)
    in z * 2 - 1

165   -- amortized rendering over several frames
data Render = Done TextureObject | Step (IO Render)

-- initial pass
flakeRenderStart :: IORef SnowGlobe -> IO Render
170   flakeRenderStart sR = do
    s0 <- readIORef sR
    p <- replicateM 4 $ randomRIO (0.02, 0.98)
    let rts = flakeTransforms p
        rho = maximum (map fst rts)
175   ts = map snd rts
    passes = clamp 4 256 . round . logBase rho $ accuracy
    loadIdentity
    ortho2D 0 1 0 1
    viewport $= (Position 0 0, Size (fromIntegral size) (fromIntegral size))

```

```

180    currentProgram $= Just (pInitial s0)
        uniform (pInitial'er s0) $= TexCoord1 (realToFrac er :: GLfloat)
        uniform (pInitial'rho s0) $= TexCoord1 (realToFrac rho :: GLfloat)
        bindFBO (fBuffer s0) (tPing s0)
        unitQuad
185    unbindFBO
        currentProgram $= Nothing
        return $ Step (flakeRenderPass sR ts passes passes)

getUniformLocation :: UniformLocation -> GLint
190 getUniformLocation (UniformLocation u) = u

-- multi step passes
flakeRenderPass :: IORef SnowGlobe -> [M3] -> N -> N -> IO Render
flakeRenderPass sR _ passes 0 = flakeRenderFinish sR passes
195 flakeRenderPass sR ts passes n = do
    s0 <- readIORef sR
    loadIdentity
    ortho2D 0 1 0 1
    viewport $= (Position 0 0, Size (fromIntegral size) (fromIntegral size))
200    currentProgram $= Just (pStep s0)
        uniform (pStep'er s0) $= TexCoord1 (realToFrac er :: GLfloat)
        uniform (pStep'src s0) $= TexCoord1 (0 :: GLint)
        withArray (map ((realToFrac :: Float -> GLfloat) . (realToFrac :: Double ->
            ↵ Float)) . concatMap matrixToList $ ts) $ glUniformMatrix3fv (↵
            ↵ getUniformLocation $ pStep'ts s0) 6 1
        bindFBO (fBuffer s0) (tPong s0)
205    textureBinding Texture2D $= Just (tPing s0)
        unitQuad
        textureBinding Texture2D $= Nothing
        unbindFBO
        writeIORef sR s0{ tPing = tPong s0, tPong = tPing s0 }
210    currentProgram $= Nothing
        if even n
            then return $ Step (flakeRenderPass sR ts passes (n - 1))
            else flakeRenderPass sR ts passes (n - 1)

215 matrixToList :: M3 -> [R]
matrixToList (M3 a b c d e f g h i) = [a,b,c,d,e,f,g,h,i]

-- colourize pass
flakeRenderFinish :: IORef SnowGlobe -> N -> IO Render
220 flakeRenderFinish sR passes = do
    s0 <- readIORef sR
    t <- newTexRGBA tSize
    bindFBO (fBuffer s0) t
    loadIdentity
225    ortho2D (-1) 1 (-1) 1
    viewport $= (Position 0 0, Size (fromIntegral tSize) (fromIntegral tSize))
    textureBinding Texture2D $= Just (tPong s0)
    currentProgram $= Just (pColour s0)
    uniform (pColour'src s0) $= TexCoord1 (0 :: GLint)
230    uniform (pColour'speed s0) $= TexCoord1 (1 / fromIntegral passes :: GLfloat)
    uniform (pColour'colour s0) $= TexCoord3 1 1 (1 :: GLfloat)
    fullQuad
    currentProgram $= Nothing
    unbindFBO

```

```

235     textureBinding Texture2D $= Just t
        glGenerateMipmap GL_TEXTURE_2D
        textureBinding Texture2D $= Nothing
        return $ Done t

240 transformRST :: R -> R -> V2 -> M3
transformRST a l (V2 x y) = M3 c s x (-s) c y 0 0 1
    where c = l * cos a
          s = l * sin a

245 flakeTransforms :: [R] -> [(R, M3)]
flakeTransforms [a,b,c,d] = [(la,inv ta),(lb,inv tb),(lc,inv tc1),(ld,inv td1),(
    ↵ lc,inv tc2),(ld,inv td2)]
    where
        lx = a + b
        ly = 2 * (c + d)
250     la = a / lx
        lb = b / lx
        lc = c / ly
        ld = d / ly
        u = V2 0 0
255     v = V2 0 la
        l = pi / 3
        ll = 2 * pi / 3
        r = -l
        rr = -ll
260     ta = transformRST 0 la u
        tb = transformRST 0 lb v
        tc1 = transformRST l lc v
        tc2 = transformRST r lc v
        td1 = transformRST ll ld v
265     td2 = transformRST rr ld v
flakeTransforms _ = error "flakeTransforms"

main :: IO ()
main = do
270     _ <- getArgsAndInitialize
        let wSize' = Size 1280 720
        initialWindowSize $= wSize'
        initialDisplayMode $= [DoubleBuffered]
        _ <- createWindow "SnowGlobe"
275     pInitial' <- shader Nothing (Just $ unlines
        [ "uniform float er;"
          , "uniform float rho;"
          , ""
          , "void main() {"
280     , "    vec2 p = er * (gl_TexCoord[0].xy * 2.0 - vec2(1.0));"
          , "    float l = length(p);"
          , "    float n;"
          , "    if (l >= er) {"
          , "        n = 0.0;"
285     , "    } else if (er > l && l >= rho * er) {"
          , "        n = (log(er) - log(l)) / -log(rho);"
          , "    } else {"
          , "        n = -1.0;"
          , "    }"
290     , "    gl_FragData[0] = vec4(n);"

```

```

    , "}"
  ])
  pInitial' er' <- get $ uniformLocation pInitial' "er"
  pInitial' rho' <- get $ uniformLocation pInitial' "rho"
295 pStep' <- shader Nothing (Just $ unlines
  [ "uniform float er;"
    , "uniform mat3 ts[6];"
    , ""
    , "uniform sampler2D src;"
    , ""
300 , "void main() {"
    , "  vec2 p0 = er * (gl_TexCoord[0].xy * 2.0 - vec2(1.0));"
    , "  float m = -1.0;"
    , "  for (int i = 0; i < 6; ++i) {"
305 , "    vec3 p = ts[i] * vec3(p0, 1.0);"
    , "    vec2 q = p.xy / p.z;"
    , "    float l = length(q);"
    , "    if (l < er) {"
    , "      m = max(m, texture2D(src, (q / er + vec2(1.0)) / 2.0).x);"
310 , "    }"
    , "  }"
    , "  if (m >= 0.0) {"
    , "    m += 1.0;"
    , "  }"
315 , "  m = max(m, texture2D(src, (p0 / er + vec2(1.0)) / 2.0).x);"
    , "  gl_FragData[0] = vec4(m);"
    , "}"
  ])
  pStep' er' <- get $ uniformLocation pStep' "er"
320 pStep' ts' <- get $ uniformLocation pStep' "ts"
  pStep' src' <- get $ uniformLocation pStep' "src"
  pColour' <- shader Nothing (Just $ unlines
  [ "uniform sampler2D src;"
    , "uniform float speed;"
325 , "uniform vec3 colour;"
    , ""
    , "void main() {"
    , "  vec2 p = gl_TexCoord[0].xy;"
    , "  float n = texture2D(src, p).x;"
330 , "  p -= vec2(0.5);"
    , "  const mat2 r = mat2(0.5, 0.8660254037844386, -0.8660254037844386, 0.5) ↵
    , "    ↵;"
    , "  for (int i = 1; i < 6; ++i) {"
    , "    p = r * p;"
    , "    n = max(n, texture2D(src, p + vec2(0.5)).x);"
335 , "  }"
    , "  if (n > 0.0) {"
    , "    n *= speed;"
    , "  } else {"
    , "    n = 0.0;"
340 , "  }"
    , "  n *= n;"
    , "  n *= n;"
    , "  gl_FragData[0] = vec4(colour, n);"
    , "}"
345 , "}"
  ])
  pColour' src' <- get $ uniformLocation pColour' "src"

```

```

pColour' speed' <- get $ uniformLocation pColour' "speed"
pColour' colour' <- get $ uniformLocation pColour' "colour"
tPing'          <- newTex size
350 tPong'        <- newTex size
fBuffer'        <- newFBO
glClampColor GL_CLAMP_VERTEX_COLOR $ fromIntegral GL_FALSE
glClampColor GL_CLAMP_READ_COLOR   $ fromIntegral GL_FALSE
glClampColor GL_CLAMP_FRAGMENT_COLOR $ fromIntegral GL_FALSE
355 sR <- newIORef SnowGlobe
    { pInitial = pInitial', pInitial'er = pInitial'er', pInitial'rho = pInitial'ρ
      ↳ rho'
      , pStep = pStep', pStep'er = pStep'er', pStep'ts = pStep'ts', pStep'src = ρ
      ↳ pStep'src'
      , pColour = pColour', pColour'src = pColour'src', pColour'speed = pColour'ρ
      ↳ speed', pColour'colour = pColour'colour'
      , tPing = tPing', tPong = tPong', fBuffer = fBuffer'
360   , sFlakes = [], sTextures = M.empty, wSize = wSize', wFullScreen = Nothing
      , sNextName = 0, sRenderFlake = return undefined
      , sRecord = False, sRecordFlakes = False
    }
modifyIORef sR $ \s' -> s' { sRenderFlake = flakeRenderStart sR }
365 addTimerCallback 40 timer
displayCallback $= display sR
reshapeCallback $= Just (reshape sR)
keyboardMouseCallback $= Just (keyboard sR)
mainLoop

370 keyboard :: IORef SnowGlobe -> Key -> KeyState -> Modifiers -> Position -> IO ()
keyboard sR (SpecialKey KeyF11) Down _ = toggleFullScreen sR
keyboard sR (Char 'f') Down _ = toggleFullScreen sR
keyboard sR (Char 'R') Down _ = modifyIORef sR $ \s -> s { sRecord = not (ρ
  ↳ sRecord s) }
375 keyboard sR (Char 'S') Down _ = modifyIORef sR $ \s -> s { sRecordFlakes = not ρ
  ↳ (sRecordFlakes s) }
keyboard _ (Char _) Down _ = exitSuccess
keyboard _ _ _ _ = return ()

toggleFullScreen :: IORef SnowGlobe -> IO ()
380 toggleFullScreen sR = do
  s <- readIORef sR
  case wFullScreen s of
    Nothing -> do
      writeIORef sR s { wFullScreen = Just (wSize s) }
385      cursor $= None
      fullScreen
    Just ws -> do
      writeIORef sR s { wFullScreen = Nothing }
      cursor $= Inherit
390      windowSize $= ws

reshape :: IORef SnowGlobe -> Size -> IO ()
reshape sR sz = do
  s <- readIORef sR
395  writeIORef sR s { wSize = sz }

timer :: IO ()
timer = do

```



```

    addTimerCallback 40 timer
400    postRedisplay Nothing

display' :: IORef SnowGlobe -> IO ()
display' sR = do
    update sR
405    s <- readIORef sR
    _ <- evaluate (sum' . map flakeName . sFlakes $ s)
    let names = S.fromList $ map flakeName (sFlakes s)
        expired = S.filter ('S.notMember' names) (M.keysSet (sTextures s))
        sTextures' = foldr M.delete (sTextures s) (S.toList expired)
410    deleteObjectNames [sTextures s M.! n | n <- S.toList expired]
    modifyIORef sR $ \s'->s'{ sTextures = sTextures' }
    r <- sRenderFlake s
    case r of
        Done t -> do
415            f <- flakeSpawn (sFlakes s) (sNextName s)
            modifyIORef sR $ \s'->s'
                { sRenderFlake = flakeRenderStart sR
                , sFlakes = f : sFlakes s'
                , sTextures = M.insert (flakeName f) t (sTextures s')
420                , sNextName = sNextName s' + 1
                }
            when (sRecordFlakes s) $
                saveTexture t ("snowglobe-" ++ show (flakeName f) ++ ".pgm")
        Step sRenderFlake' ->
425            modifyIORef sR $ \s'->s'{ sRenderFlake = sRenderFlake' }

update :: IORef SnowGlobe -> IO ()
update sR = do
    s <- readIORef sR
430    let sFlakes' = flakesUpdate (1 / 256) (sFlakes s)
        writeIORef sR (s{ sFlakes = sFlakes' })

display :: IORef SnowGlobe -> IO ()
display sR = do
435    s <- readIORef sR
    loadIdentity
    let Size w h = wSize s
        r = 0.7
        (x, y)
440        | h < w      = (r, r * fromIntegral h / fromIntegral w)
        | otherwise = (r * fromIntegral w / fromIntegral h, r)
    ortho2D (-x) x (-y) y
    viewport $= (Position 0 0, wSize s)
    clearColor $= Color4 0 0 0.25 1
445    clear [ColorBuffer]
    texture Texture2D $= Enabled
    blend $= Enabled
    blendFunc $= (SrcAlpha, OneMinusSrcAlpha)
    forM_ (sFlakes s) (flakeDraw s)
450    blend $= Disabled
    texture Texture2D $= Disabled
    swapBuffers
    when (sRecord s) $ hPut stdout ==<< capturePPM
    reportErrors
455    display' sR

```

```

flakeDraw :: SnowGlobe -> Flake -> IO ()
flakeDraw s f = do
  let d :: GLdouble
460   d = realToFrac $ flakeSize f / 4
      a :: GLdouble
      a = realToFrac $ 360 * flakeTime f * sin (fromIntegral (flakeName f))
      p :: GLdouble -> GLdouble -> IO ()
      p u v = do
465       texCoord $ TexCoord2 ((1+u)/2) ((1+v)/2)
       vertex $ Vertex2 u v
      V2 x y = flakePosition f
  case flakeName f 'M.lookup' sTextures s of
    Nothing -> return ()
470   t -> do
      textureBinding Texture2D $= t
      unsafePreservingMatrix $ do
        translate $ Vector3 (realToFrac x :: GLdouble) (realToFrac y :: GLdouble)
          ↵ ) 0
        rotate a (Vector3 0 0 1)
475       GL.scale d d d
        renderPrimitive Quads $ p (-1) (-1) >> p 1 (-1) >> p 1 1 >> p (-1) 1
      textureBinding Texture2D $= Nothing

newTex :: N -> IO TextureObject
480 newTex s = do
  [t] <- genObjectNames 1
  textureBinding Texture2D $= Just t
  glTexImage2D GL_TEXTURE2D 0 (fromIntegral GL_R32F) (fromIntegral s) (↵
    ↵ fromIntegral s) 0 GL_RED GL_UNSIGNED_BYTE nullPtr
  textureFilter Texture2D $= ((Linear', Nothing), Linear')
485 textureWrapMode Texture2D S $= (Repeated, ClampToEdge)
  textureWrapMode Texture2D T $= (Repeated, ClampToEdge)
  textureBinding Texture2D $= Nothing
  return t

490 newTexRGBA :: N -> IO TextureObject
newTexRGBA s = do
  [t] <- genObjectNames 1
  textureBinding Texture2D $= Just t
  glTexImage2D GL_TEXTURE2D 0 (fromIntegral GL_RGBA) (fromIntegral s) (↵
    ↵ fromIntegral s) 0 GL_RGBA GL_UNSIGNED_BYTE nullPtr
495 textureFilter Texture2D $= ((Linear', Just Linear'), Linear')
  textureWrapMode Texture2D S $= (Repeated, ClampToEdge)
  textureWrapMode Texture2D T $= (Repeated, ClampToEdge)
  textureBinding Texture2D $= Nothing
  return t

500
saveTexture :: TextureObject -> FilePath -> IO ()
saveTexture t f = withBinaryFile f WriteMode $ \h -> do
  let header = "P5\n" ++ show tSize ++ " " ++ show tSize ++ "\n255\n"
      n = tSize * tSize
505   hPutStr h header
  allocaArray n $ \p -> do
    textureBinding Texture2D $= Just t
    glGetTexImage GL_TEXTURE2D 0 GL_ALPHA GL_UNSIGNED_BYTE (p :: Ptr Word8)
    textureBinding Texture2D $= Nothing

```

```

510     hPutBuf h p n

newtype FramebufferObject = FramebufferObject GLuint

newFBO :: IO FramebufferObject
515 newFBO = fmap FramebufferObject (alloca $ \p -> glGenFramebuffers 1 p >> peek p)

bindFBO :: FramebufferObject -> TextureObject -> IO ()
bindFBO (FramebufferObject f) (TextureObject t) = do
    glBindFramebuffer GLFRAMEBUFFER f
520    glFramebufferTexture2D GLFRAMEBUFFER GLCOLOR_ATTACHMENT0 GLTEXTURE_2D t 0

unbindFBO :: IO ()
unbindFBO = do
    glFramebufferTexture2D GLFRAMEBUFFER GLCOLOR_ATTACHMENT0 GLTEXTURE_2D 0 0
525    glBindFramebuffer GLFRAMEBUFFER 0

fullQuad :: IO ()
fullQuad = do
    renderPrimitive Quads $ do
530        t (0.5-r) (0.5+r) >> v (-r2) ( r2)
        t (0.5-r) (0.5-r) >> v (-r2) (-r2)
        t (0.5+r) (0.5-r) >> v ( r2) (-r2)
        t (0.5+r) (0.5+r) >> v ( r2) ( r2)
    where
535        r = sqrt 0.5 / realToFrac er
        r2 = 1
        t, v :: GLdouble -> GLdouble -> IO ()
        t x y = texCoord (TexCoord2 x y)
        v x y = vertex (Vertex2 x y)
540
unitQuad :: IO ()
unitQuad = renderPrimitive Quads $ do
    t 0 1 >> v 0 1
    t 0 0 >> v 0 0
545    t 1 0 >> v 1 0
    t 1 1 >> v 1 1
    where
        t, v :: GLdouble -> GLdouble -> IO ()
        t x y = texCoord (TexCoord2 x y)
550    v x y = vertex (Vertex2 x y)

clamp :: Ord a => a -> a -> a -> a
clamp mi ma x = mi 'max' x 'min' ma

```

## 10 Vector.hs

```
{-# LANGUAGE MultiParamTypeClasses, TypeSynonymInstances #-}
```

```
module Vector where
```

```

5  type R = Double

data V1 = V1 !R deriving (Show, Eq, Ord)
data V2 = V2 !R !R deriving (Show, Eq, Ord)
data V3 = V3 !R !R !R deriving (Show, Eq, Ord)
10 data V4 = V4 !R !R !R !R deriving (Show, Eq, Ord)

```

```

class V a where
  o      :: a
  (^+)   :: a -> a -> a
  15  (^-) :: a -> a -> a
  (*^)   :: R -> a -> a
  (^*)   :: a -> R -> a
  (^/)   :: a -> R -> a
  dot    :: a -> a -> R
20
  (|-|)  :: V a => a -> a -> R
  u |-| v = let d = u ^-^ v in d `dot` d

norm :: V a => a -> a
25 norm v = v ^/ sqrt (v `dot` v)

instance V V1 where
  o = V1 0
  V1 a ^+^ V1 x = V1 (a + x)
  30 V1 a ^-^ V1 x = V1 (a - x)
  k *^ V1 x = V1 (k * x)
  V1 a ^* k = V1 (a * k)
  V1 a ^/ k = V1 (a / k)
  V1 a `dot` V1 x = a * x
35

instance V V2 where
  o = V2 0 0
  V2 a b ^+^ V2 x y = V2 (a + x) (b + y)
  V2 a b ^-^ V2 x y = V2 (a - x) (b - y)
  40 k *^ V2 x y = V2 (k * x) (k * y)
  V2 a b ^* k = V2 (a * k) (b * k)
  V2 a b ^/ k = V2 (a / k) (b / k)
  V2 a b `dot` V2 x y = a * x + b * y

45 instance V V3 where
  o = V3 0 0 0
  V3 a b c ^+^ V3 x y z = V3 (a + x) (b + y) (c + z)
  V3 a b c ^-^ V3 x y z = V3 (a - x) (b - y) (c - z)
  k *^ V3 x y z = V3 (k * x) (k * y) (k * z)
  50 V3 a b c ^* k = V3 (a * k) (b * k) (c * k)
  V3 a b c ^/ k = V3 (a / k) (b / k) (c / k)
  V3 a b c `dot` V3 x y z = a * x + b * y + c * z

cross3 :: V3 -> V3 -> V3
55 cross3 (V3 a1 a2 a3) (V3 b1 b2 b3) =
  V3 (a2*b3-a3*b2) (a3*b1-a1*b3) (a1*b2-a2*b1)

instance V V4 where
  o = V4 0 0 0 0
  60 V4 a b c d ^+^ V4 x y z w = V4 (a + x) (b + y) (c + z) (d + w)
  V4 a b c d ^-^ V4 x y z w = V4 (a - x) (b - y) (c - z) (d - w)
  k *^ V4 x y z w = V4 (k * x) (k * y) (k * z) (k * w)
  V4 a b c d ^* k = V4 (a * k) (b * k) (c * k) (d * k)
  V4 a b c d ^/ k = V4 (a / k) (b / k) (c / k) (d / k)
  65 V4 a b c d `dot` V4 x y z w = a * x + b * y + c * z + d * w

data M1 = M1 !R deriving (Show, Eq, Ord)

```

```

data M2 = M2 !R !R !R !R deriving (Show, Eq, Ord)
data M3 = M3 !R !R !R !R !R !R !R !R !R !R deriving (Show, Eq, Ord)
70 data M4 = M4 !R !R !R !R !R !R !R !R !R !R !R !R !R !R !R !R deriving (Show, Eq, Ord)
    ↳ Eq, Ord)

class M a where
    i      :: a
    (^^+)  :: a -> a -> a
75    (^^-)  :: a -> a -> a
    (^^*)  :: a -> a -> a
    (*^^)  :: R -> a -> a
    (^^*)  :: a -> R -> a
    (^^/)  :: a -> R -> a
80    mdot   :: a -> a -> R
    det     :: a -> R
    inv     :: a -> a

(||-||) :: M a => a -> a -> R
85 u ||-|| v = let d = u ^^+^^ v in d `mdot` d

instance M M1 where
    i = M1 1
    M1 a11 ^^+^^ M1 b11 = M1 (a11 + b11)
90    M1 a11 ^^+^^ M1 b11 = M1 (a11 - b11)
    M1 a11 ^^*^^ M1 b11 = M1 (a11 * b11)
    a *^^ M1 b11 = M1 (a * b11)
    M1 a11 ^^* b = M1 (a11 * b)
    M1 a11 ^^/ b = M1 (a11 / b)
95    M1 a11 `mdot` M1 b11 = (a11 * b11)
    det (M1 a11) = a11
    inv (M1 a11) = M1 (1/a11)

instance M M2 where
100    i = M2 1 0 0 1
    M2 a11 a12 a21 a22 ^^+^^ M2 b11 b12 b21 b22 =
        M2 (a11 + b11) (a12 + b12) (a21 + b21) (a22 + b22)
    M2 a11 a12 a21 a22 ^^+^^ M2 b11 b12 b21 b22 =
        M2 (a11 - b11) (a12 - b12) (a21 - b21) (a22 - b22)
105    M2 a11 a12 a21 a22 ^^*^^ M2 b11 b12 b21 b22 =
        M2 (a11*b11 + a12*b21) (a11*b12 + a12*b22) (a21*b11 + a22*b21) (a21*b12 +
        ↳ a22*b22)
    a *^^ M2 b11 b12 b21 b22 = M2 (a * b11) (a * b12) (a * b21) (a * b22)
    M2 a11 a12 a21 a22 ^^* b = M2 (a11 * b) (a12 * b) (a21 * b) (a22 * b)
    M2 a11 a12 a21 a22 ^^/ b = M2 (a11 / b) (a12 / b) (a21 / b) (a22 / b)
110    M2 a11 a12 a21 a22 `mdot` M2 b11 b12 b21 b22 =
        a11*b11 + a12*b12 + a21*b21 + a22*b22
    det (M2 a11 a12 a21 a22) = a11 * a22 - a12 * a21
    inv a@(M2 a11 a12 a21 a22) = (M2 a22 (-a12) (-a21) a11) ^^/ det a

115 instance M M3 where
    i = M3 1 0 0 0 1 0 0 0 1
    M3 a11 a12 a13 a21 a22 a23 a31 a32 a33 ^^+^^ M3 b11 b12 b13 b21 b22 b23 b31 b32 b33 =
        ↳ b32 b33 =
        M3 (a11 + b11) (a12 + b12) (a13 + b13) (a21 + b21) (a22 + b22) (a23 + b23) (
        ↳ a31 + b31) (a32 + b32) (a33 + b33)
    M3 a11 a12 a13 a21 a22 a23 a31 a32 a33 ^^+^^ M3 b11 b12 b13 b21 b22 b23 b31 b32 b33 =
        ↳ b32 b33 =

```

```

120      M3 (a11 - b11) (a12 - b12) (a13 - b13) (a21 - b21) (a22 - b22) (a23 - b23) (↵
        ↵ a31 - b31) (a32 - b32) (a33 - b33)
M3 a11 a12 a13 a21 a22 a23 a31 a32 a33 ^*^^ M3 b11 b12 b13 b21 b22 b23 b31 ↵
        ↵ b32 b33 =
      M3 (a11*b11 + a12*b21 + a13*b31) (a11*b12 + a12*b22 + a13*b32) (a11*b13 + ↵
        ↵ a12*b23 + a13*b33)
        (a21*b11 + a22*b21 + a23*b31) (a21*b12 + a22*b22 + a23*b32) (a21*b13 + ↵
        ↵ a22*b23 + a23*b33)
        (a31*b11 + a32*b21 + a33*b31) (a31*b12 + a32*b22 + a33*b32) (a31*b13 + ↵
        ↵ a32*b23 + a33*b33)
125      a *^^ M3 b11 b12 b13 b21 b22 b23 b31 b32 b33 =
      M3 (a * b11) (a * b12) (a * b13) (a * b21) (a * b22) (a * b23) (a * b31) (a ↵
        ↵ * b32) (a * b33)
M3 a11 a12 a13 a21 a22 a23 a31 a32 a33 ^* b =
      M3 (a11 * b) (a12 * b) (a13 * b) (a21 * b) (a22 * b) (a23 * b) (a31 * b) (↵
        ↵ a32 * b) (a33 * b)
M3 a11 a12 a13 a21 a22 a23 a31 a32 a33 ^/ b =
130      M3 (a11 / b) (a12 / b) (a13 / b) (a21 / b) (a22 / b) (a23 / b) (a31 / b) (↵
        ↵ a32 / b) (a33 / b)
M3 a11 a12 a13 a21 a22 a23 a31 a32 a33 'mdot' M3 b11 b12 b13 b21 b22 b23 b31 ↵
        ↵ b32 b33 =
      a11*b11 + a12*b12 + a13*b13 +
      a21*b21 + a22*b22 + a23*b23 +
      a31*b31 + a32*b32 + a33*b33
135      det (M3 a11 a12 a13 a21 a22 a23 a31 a32 a33) =
      let m11 = M2 a22 a23 a32 a33
          m12 = M2 a21 a23 a31 a33
          m13 = M2 a21 a22 a31 a32
      in a11 * det m11 - a12 * det m12 + a13 * det m13
140      inv a@(M3 a11 a12 a13 a21 a22 a23 a31 a32 a33) =
      let m11 = a33 * a22 - a32 * a23
          m12 = -(a33 * a12 - a32 * a13)
          m13 = a23 * a12 - a22 * a13
          m21 = -(a33 * a21 - a31 * a23)
          m22 = a33 * a11 - a31 * a13
          m23 = -(a23 * a11 - a21 * a13)
          m31 = a32 * a21 - a31 * a22
          m32 = -(a32 * a11 - a31 * a12)
          m33 = a22 * a11 - a21 * a12
145      in (M3 m11 m12 m13 m21 m22 m23 m31 m32 m33) ^^/ det a

instance M M4 where
  i = M4 1 0 0 0 0 1 0 0 0 0 1 0 0 0 0 1
  M4 a11 a12 a13 a14 a21 a22 a23 a24 a31 a32 a33 a34 a41 a42 a43 a44 ^+^^ M4 ↵
        ↵ b11 b12 b13 b14 b21 b22 b23 b24 b31 b32 b33 b34 b41 b42 b43 b44 =
155      M4 (a11 + b11) (a12 + b12) (a13 + b13) (a14 + b14)
        (a21 + b21) (a22 + b22) (a23 + b23) (a24 + b24)
        (a31 + b31) (a32 + b32) (a33 + b33) (a34 + b34)
        (a41 + b41) (a42 + b42) (a43 + b43) (a44 + b44)
      M4 a11 a12 a13 a14 a21 a22 a23 a24 a31 a32 a33 a34 a41 a42 a43 a44 ^^--^^ M4 ↵
        ↵ b11 b12 b13 b14 b21 b22 b23 b24 b31 b32 b33 b34 b41 b42 b43 b44 =
160      M4 (a11 - b11) (a12 - b12) (a13 - b13) (a14 - b14)
        (a21 - b21) (a22 - b22) (a23 - b23) (a24 - b24)
        (a31 - b31) (a32 - b32) (a33 - b33) (a34 - b34)
        (a41 - b41) (a42 - b42) (a43 - b43) (a44 - b44)
      M4 a11 a12 a13 a14 a21 a22 a23 a24 a31 a32 a33 a34 a41 a42 a43 a44 ^*^^ M4 ↵
        ↵ b11 b12 b13 b14 b21 b22 b23 b24 b31 b32 b33 b34 b41 b42 b43 b44 =

```

```

165      M4 (a11*b11 + a12*b21 + a13*b31 + a14*b41) (a11*b12 + a12*b22 + a13*b32 + ↵
          ↵ a14*b42) (a11*b13 + a12*b23 + a13*b33 + a14*b43) (a11*b14 + a12*b24 + ↵
          ↵ a13*b34 + a14*b44)
          (a21*b11 + a22*b21 + a23*b31 + a24*b41) (a21*b12 + a22*b22 + a23*b32 + ↵
          ↵ a24*b42) (a21*b13 + a22*b23 + a23*b33 + a24*b43) (a21*b14 + a22*b24 ↵
          ↵ + a23*b34 + a24*b44)
          (a31*b11 + a32*b21 + a33*b31 + a34*b41) (a31*b12 + a32*b22 + a33*b32 + ↵
          ↵ a34*b42) (a31*b13 + a32*b23 + a33*b33 + a34*b43) (a31*b14 + a32*b24 ↵
          ↵ + a33*b34 + a34*b44)
          (a41*b11 + a42*b21 + a43*b31 + a44*b41) (a41*b12 + a42*b22 + a43*b32 + ↵
          ↵ a44*b42) (a41*b13 + a42*b23 + a43*b33 + a44*b43) (a41*b14 + a42*b24 ↵
          ↵ + a43*b34 + a44*b44)
a *^^ M4 b11 b12 b13 b14 b21 b22 b23 b24 b31 b32 b33 b34 b41 b42 b43 b44 =
170      M4 (a * b11) (a * b12) (a * b13) (a * b14)
          (a * b21) (a * b22) (a * b23) (a * b24)
          (a * b31) (a * b32) (a * b33) (a * b34)
          (a * b41) (a * b42) (a * b43) (a * b44)
M4 a11 a12 a13 a14 a21 a22 a23 a24 a31 a32 a33 a34 a41 a42 a43 a44 ^* b =
175      M4 (a11 * b) (a12 * b) (a13 * b) (a14 * b)
          (a21 * b) (a22 * b) (a23 * b) (a24 * b)
          (a31 * b) (a32 * b) (a33 * b) (a34 * b)
          (a41 * b) (a42 * b) (a43 * b) (a44 * b)
M4 a11 a12 a13 a14 a21 a22 a23 a24 a31 a32 a33 a34 a41 a42 a43 a44 ^/ b =
180      M4 (a11 / b) (a12 / b) (a13 / b) (a14 / b)
          (a21 / b) (a22 / b) (a23 / b) (a24 / b)
          (a31 / b) (a32 / b) (a33 / b) (a34 / b)
          (a41 / b) (a42 / b) (a43 / b) (a44 / b)
M4 a11 a12 a13 a14 a21 a22 a23 a24 a31 a32 a33 a34 a41 a42 a43 a44 'mdot' M4 ↵
          ↵ b11 b12 b13 b14 b21 b22 b23 b24 b31 b32 b33 b34 b41 b42 b43 b44 =
185      a11*b11 + a12*b12 + a13*b13 + a14*b14 +
          a21*b21 + a22*b22 + a23*b23 + a24*b24 +
          a31*b31 + a32*b32 + a33*b33 + a34*b34 +
          a41*b41 + a42*b42 + a43*b43 + a44*b44
det (M4 a11 a12 a13 a14 a21 a22 a23 a24 a31 a32 a33 a34 a41 a42 a43 a44) =
190      let m11 = M3 a22 a23 a24 a32 a33 a34 a42 a43 a44
          m12 = M3 a21 a23 a24 a31 a33 a34 a41 a43 a44
          m13 = M3 a21 a22 a24 a31 a32 a34 a41 a42 a44
          m14 = M3 a21 a22 a23 a31 a32 a33 a41 a42 a43
          in a11 * det m11 - a12 * det m12 + a13 * det m13 - a14 * det m14
195      inv (M4 a11 a12 a13 a14 a21 a22 a23 a24 a31 a32 a33 a34 a41 a42 a43 a44) =
          let a = M2 a11 a12 a21 a22
              b = M2 a13 a14 a23 a24
              c = M2 a31 a32 a41 a42
              d = M2 a33 a34 a43 a44
200              a1 = inv a
              ca1 = c ^^*^^ a1
              dcab1 = inv (d ^^-^^ (ca1 ^^*^^ b))
              a1bdcab1 = a1 ^^*^^ (b ^^*^^ dcab1)
              M2 m11 m12 m21 m22 = a1 ^^+^^ (a1bdcab1 ^^*^^ ca1)
205              M2 m13 m14 m23 m24 = (-1) ^^*^^ a1bdcab1
              M2 m31 m32 m41 m42 = (-1) ^^*^^ (dcab1 ^^*^^ ca1)
              M2 m33 m34 m43 m44 = dcab1
          in M4 m11 m12 m13 m14 m21 m22 m23 m24 m31 m32 m33 m34 m41 m42 m43 m44

210 class MV m v where
      (^*^) :: m -> v -> v
      (^*!) :: v -> v -> m

```

```

215 reflector :: (M m, V v, MV m v) => v -> m
    reflector v = i ^- ^- (2 * ^- (v ^* ^! v))

instance MV M1 V1 where
    M1 m ^* ^ V1 v = V1 (m * v)
    V1 a ^* ^! V1 b = M1 (a * b)

220 instance MV M2 V2 where
    M2 m11 m12 m21 m22 ^* ^ V2 v1 v2 =
        V2 (m11*v1 + m12*v2)
            (m21*v1 + m22*v2)
225 V2 a1 a2 ^* ^! V2 b1 b2 =
    M2 (a1 * b1) (a1 * b2)
        (a2 * b1) (a2 * b2)

instance MV M3 V3 where
230 M3 m11 m12 m13 m21 m22 m23 m31 m32 m33 ^* ^ V3 v1 v2 v3 =
    V3 (m11*v1 + m12*v2 + m13*v3)
        (m21*v1 + m22*v2 + m23*v3)
        (m31*v1 + m32*v2 + m33*v3)
    V3 a1 a2 a3 ^* ^! V3 b1 b2 b3 =
235 M3 (a1 * b1) (a1 * b2) (a1 * b3)
        (a2 * b1) (a2 * b2) (a2 * b3)
        (a3 * b1) (a3 * b2) (a3 * b3)

instance MV M4 V4 where
240 M4 m11 m12 m13 m14 m21 m22 m23 m24 m31 m32 m33 m34 m41 m42 m43 m44 ^* ^ V4 v1 v2 v3 v4 =
    V4 (m11*v1 + m12*v2 + m13*v3 + m14*v4)
        (m21*v1 + m22*v2 + m23*v3 + m24*v4)
        (m31*v1 + m32*v2 + m33*v3 + m34*v4)
        (m41*v1 + m42*v2 + m43*v3 + m44*v4)
245 V4 a1 a2 a3 a4 ^* ^! V4 b1 b2 b3 b4 =
    M4 (a1 * b1) (a1 * b2) (a1 * b3) (a1 * b4)
        (a2 * b1) (a2 * b2) (a2 * b3) (a2 * b4)
        (a3 * b1) (a3 * b2) (a3 * b3) (a3 * b4)
        (a4 * b1) (a4 * b2) (a4 * b3) (a4 * b4)

250 cross4 :: V4 -> V4 -> V4 -> V4
    cross4 (V4 u0 u1 u2 u3) (V4 v0 v1 v2 v3) (V4 w0 w1 w2 w3) =
    {-
255 let vw01 = v0 * w1 - v1 * w0
        vw02 = v0 * w2 - v2 * w0
        vw03 = v0 * w3 - v3 * w0
        vw12 = v1 * w2 - v2 * w1
        vw13 = v1 * w3 - v3 * w1
        vw23 = v2 * w3 - v3 * w2
260 r0 = u1 * vw23 - u2 * vw13 + u3 * vw12
        r1 = - u0 * vw23 + u2 * vw03 - u3 * vw02
        r2 = u0 * vw13 - u1 * vw03 + u3 * vw02
        r3 = - u0 * vw12 + u1 * vw02 - u2 * vw01
    in V4 r0 r1 r2 r3
265 -}
    let m0 = M3 u1 u2 u3 v1 v2 v3 w1 w2 w3
        m1 = M3 u0 u2 u3 v0 v2 v3 w0 w2 w3
        m2 = M3 u0 u1 u3 v0 v1 v3 w0 w1 w3

```



```
270      m3 = M3 u0 u1 u2 v0 v1 v2 w0 w1 w2
      in V4 (det m0) (-(det m1)) (det m2) (-(det m3))
```